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Liu, Chunhua; Chau, K. T.

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Article

# Electromagnetic Design of a New Electrically Controlled Magnetic Variable-Speed Gearing Machine

Chunhua Liu \* and K. T. Chau

Department of Electrical and Electronic Engineering, The University of Hong Kong, Hong Kong, China;  
E-Mail: ktchau@eee.hku.hk

\* Author to whom correspondence should be addressed; E-Mail: chualiu@eee.hku.hk;  
Tel.: +852-2859-2687; Fax: +852-2559-8738.

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**Abstract:** This paper proposes a new electrically controlled magnetic variable-speed gearing (EC-MVSG) machine, which is capable of providing controllable gear ratios for hybrid electric vehicle (HEV) applications. The key design feature involves the adoption of a magnetic gearing structure and acceptance of the memory machine flux-mnemonic concept. Hence, the proposed machine can not only offer a gear-shifting mechanism for torque and speed transmission, but also provide variable gear ratios for torque and speed variation. The electromagnetic design is studied and discussed. The finite-element method is developed with the hysteresis model to verify the validity of the machine design.

**Keywords:** magnetic gear; memory machine; permanent-magnet (PM) machine; hysteresis model; finite element method; electrically controlled gear ratio; hybrid electric vehicle (HEV)

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## 1. Introduction

Electric machines, which play the essential role of electromechanical energy conversion, are one of the most important components of electric vehicles (EVs) and hybrid EVs (HEVs) [1–3]. In recent years, different emerging energy conversion technologies have been proposed for HEVs, such as the integrated-starter-generator (ISG), in-wheel motor drive (IWMD), electronic continuously variable transmission (E-CVT), and so on [4–6]. All these new machines possess distinct merits which effectively improve the vehicle characteristics and significantly address the various electricity issues.

In the power train of vehicles, mechanical gearing sets have been widely used in modern industrial applications for torque and speed transmission. However, they suffer from the inherent drawbacks of mechanical gears (wear-and tear, annoying noise and need for regular maintenance) and the problems of gearboxes (high transmission losses, bulky size, heavy weight and complicated gear-shifting mechanisms). Recently, magnetic gearing sets (magnetic gears and magnetic gearing machines) have been actively developed. Based on the permanent-magnet (PM) attraction for torque transmission, they naturally display the merits of contactless transmission, silent operation and maintenance free, hence solving the drawbacks of mechanical gears [7–9]. Very recently, magnetic gears and magnetic gearing machines have been attempted to take place of mechanical gearing sets with fixed gearing ratios for wind power generation and EV applications [10–12].

Nevertheless, a direct replacement of mechanical gearboxes by magnetic gearing sets with the aim of offering controllable gear ratios is still lacking. Controllable gear ratios are highly desirable for practical applications, such as acting as electric variable transmissions or so-called E-CVTs for HEVs and extended to planetary-gear E-CVTs and dual-machine E-CVTs for HEV or wind power generation [13–16]. All these E-CVT systems require one or more sets of mechanical planetary gears which still inevitably involve the known drawbacks of mechanical gears. Although some attempts were performed with magnetic gear sets for E-CVTs or extended for other applications [17–19], they still have complicated structures and complex control strategies due to their fixed gear ratios.

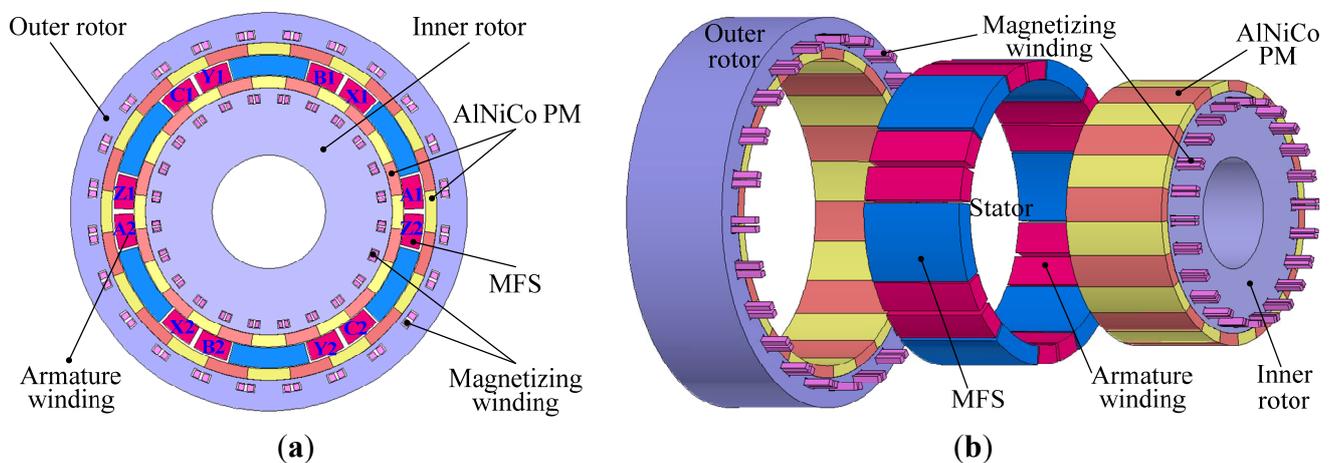
Recently, a new breed of flux-controllable PM brushless machines, called memory machines, which have the distinct capability to tune the PM magnetization and memorize it, has emerged with considerable attention. In [20,21], the memory machine is proposed for using the armature currents to magnetize the aluminum-nickel-cobalt (AlNiCo) PMs into different magnetization levels, but this kind of alternating current (AC)-excited memory machines are easily demagnetized by accidental armature currents and their armature current control is relatively complicated. In [22,23], by applying coordinate direct current (DC) pulse currents to magnetize the AlNiCo PMs, a DC-excited memory machine was developed which can effectively overcome the shortcomings of the AC-excited type. Although the flux-mnemonic concept of memory machines has attracted increasing attention, development has just focused on their design topologies and control strategies. An extension of this flux-mnemonic concept to the field of magnetic gearing is still absent in the literature. Also, it is worth mentioning that AlNiCo PMs are not rare-earth PMs, which can be much more cost-effective than rare-earth PMs, such as neodymium-iron-boron (NdFeB) PMs.

The purpose of this paper is to propose a new electrically controlled magnetic variable-speed gearing (EC-MVSG) machine, which can provide controllable gear ratios for HEV applications. Different from the mechanical gearing systems, the proposed machine adopts the magnetic gearing structure and accepts the memory machine flux-mnemonic concept. Hence, the proposed machine can not only offer a gearing mechanism for torque and speed transmission, but also provide variable gear ratios for torque and speed variation. Specifically, the proposed machine will use the topology with two rotors and a stator. Different from the multi-layer airgap structure of existing magnetic gearing machines [10,11], this topology has only two effective airgaps for electromagnetic energy conversion. The machine design and operation principle will be introduced and discussed in detail. Also, the corresponding performance will be analyzed by using the time-stepping finite element method (TS-FEM).

## 2. Machine Design

Figure 1 shows the configuration of the proposed EC-MVSG machine, which is the combination of the concepts of the magnetic gearing machine and the memory machine. First, the proposed machine comprises of an outer rotor, an inner rotor and a stator. Both rotor surfaces have 24-pole AlNiCo PMs, which can be independently magnetized and demagnetized. The sandwiched stator is composed of modulated ferromagnetic segments (MFSs) and armature windings. With this topology, the proposed machine can modulate the inner rotor rotating field and the outer rotor rotating field by the MFSs, hence achieving the magnetic gearing effect. Then, since the number of AlNiCo PM pole-pairs of the inner and outer rotors can be flexibly adjusted by the adjacent magnetizing windings, the magnetic gear ratios can be correspondingly changed. In addition, since these magnetizing windings only need to carry temporary current pulses to magnetize or demagnetize the PMs, they are small enough to be embedded into the rotor yoke. This machine is relatively complicated when compared with the traditional PM machines with one airgap [1,2], but the structure is not complicated when compared with those integrated machines with two or three airgaps [5,14,18]. Also, in order to keep the coils away from the inner and outer rotating parts, a good alignment is necessary; otherwise, additional mechanical shield layers will be required, which will increase the airgap length and decrease the machine performance.

**Figure 1.** Proposed electrically controlled magnetic variable-speed gearing (EC-MVSG) machine: (a) structure view; and (b) component view. AlNiCo: aluminum-nickel-cobalt; PM: permanent-magnet; and MFS: modulated ferromagnetic segment.



Since the proposed EC-MVSG machine integrates two distinct concepts of magnetic gearing and flux-mnemonics, it has many unique features as follows:

- The whole structure is compact and robust, and fully utilizes the machine space for accommodating PMs, windings and MFSs. Both rotors have PMs and magnetizing windings, which means both pole-pairs of rotors can be adjusted. The stator not only comprises MFSs, but also artfully incorporates the MFSs into the air space. In this way, although two concepts are created for the machine design, the flux path is very short from the inner rotor to the outer rotor, and armature windings are bypassed, therefore, it can greatly improve the flux transmission efficiency.

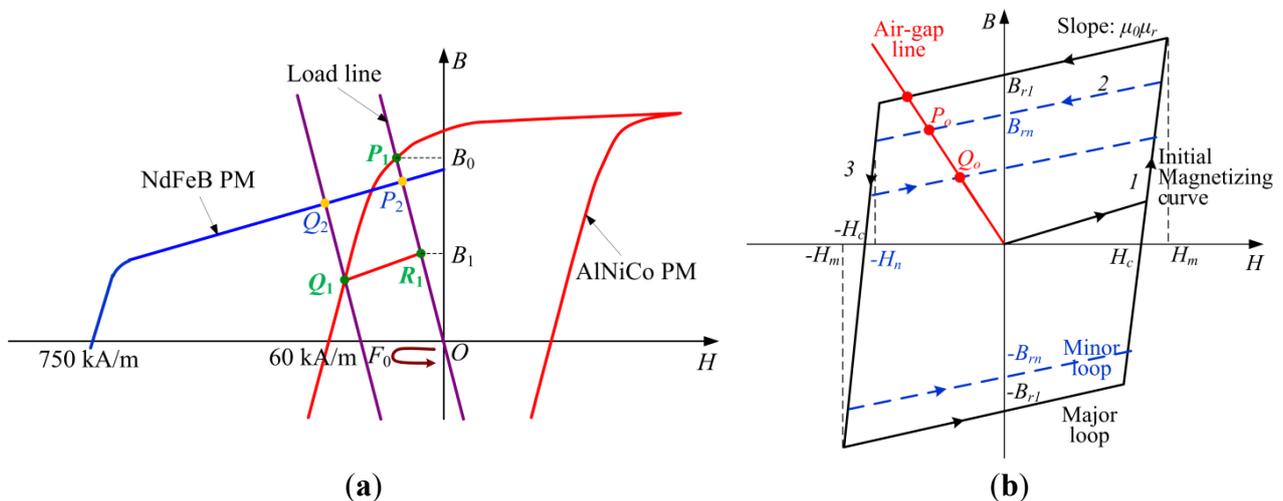
- The stator is quite different from those magnetic gearing machines which have separate two parts for the MFSs and the armature windings [10,11]. It integrates MFSs and armature windings together, hence effectively decreasing the machine size and improving the power density.
- Both rotors accommodate PMs and magnetizing windings, which inherently create the flux-mnemonic feature for PM pole-pairs. Also, it can be found that the rotor space is fully utilized, hence further increasing the material cost-effectiveness. In addition, these 24 pieces of PMs in both rotors can be magnetized or demagnetized to the desired applicable pole-pairs, such as two and four.
- The AlNiCo PM is not a rare-earth PM and hence is more abundant and cheap. In addition, it should be noted that two sets of slip rings are needed to access the magnetizing windings of both rotors.
- The proposed machine has the capability of gearing effect (with fixed gear ratio) for changing the torque and speed. Namely, if the inner rotor runs at high speed with low-torque output, the outer rotor can run at low speed with high-torque output under a fixed gear ratio.
- The proposed machine also has the capability of variable gear ratios for torque and speed variation. Namely, the proposed machine has three gear ratios for its outer-rotor speed over its inner-rotor speed, such as 1:1,  $-2:1$  and  $-1/2$ .

### 3. Machine Operation Principle

#### 3.1. Hysteresis Model of the AlNiCo PM

The AlNiCo PM, created in the 1930s, was widely applied for PM machines due to its high remanence, high thermal stability and high stability [23]. However, the AlNiCo PM has a low coercivity, which easily leads to irreversible demagnetization under unexpected extreme operating conditions. Also, its nonlinear demagnetization curve makes it never superpose on the same recoil line, which means it having unfixed recoil lines for different magnetization levels. As a result, NdFeB PMs with the high coercivity and linear demagnetization curves are currently preferred for PM machines. Figure 2a shows their corresponding  $B$ - $H$  curves.

**Figure 2.** Operating principle of different PMs: (a)  $B$ - $H$  curves; and (b) proposed hysteresis model of AlNiCo PM. NdFeB: neodymium-iron-boron.



On the other hand, the AlNiCo PM is suitable for memory machines because of its nonlinear demagnetization characteristics. That is, once the demagnetization current is added for a short time and then removed, the operation point will move along the recoil line and stay at a lower magnetization level. It also means that the magnetization level is memorized. As shown in Figure 2b, the AlNiCo PM adopts a parallelogram hysteresis model for this machine design [23]. Its piecewise-linear feature makes it close with the true model and convenient for time-stepping finite-element calculations. It shows that the major hysteresis loop and all the minor hysteresis loops have the same value of coercivity  $-H_c$ , but they have different values of remanence  $B_m$ .

In detail, the main beelines that represent the magnetizing and demagnetizing processes are marked in Figure 2b with 1, 2 and 3. During the magnetizing process, the operating point moves upward along the Line 1, then leftward along the Line 2, and stays at the operating point of  $P_o$ . Subsequently, during the demagnetizing process, the operating point moves leftward along the Line 2, then downward along the Line 3, then rightward along the recoil line until settling at the operating point of  $Q_o$  with a lower flux level. The corresponding equations of these beelines can be respectively expressed as [21–23]:

$$\text{Line 1: } B = \frac{\mu_r \mu_0 H_m + B_{r1}}{H_m - H_c} (H - H_c) \quad (1)$$

$$\text{Line 2: } B = \mu_r \mu_0 H_m + B_{rn}, \quad n = 1, 2, 3 \dots \quad (2)$$

$$\text{Line 3: } B = \frac{\mu_r \mu_0 H_m + B_{r1}}{H_m - H_c} (H + H_c) \quad (3)$$

where  $\mu_0$  is the vacuum permeability;  $\mu_r$  is the relative permeability;  $H_m$  is the saturated magnetic field intensity; and  $B_m$  denotes the remanence of the  $n$ -th hysteresis loop. By using Equations (2) and (3), the value of  $H_n$  at the vertex of the  $n$ -th loop can be achieved as follows:

$$H_n = \frac{(H_m - H_c)B_m - H_c(\mu_0 \mu_r H_m + B_{r1})}{\mu_0 \mu_r H_c + B_{r1}}, \quad n = 1, 2, 3 \dots \quad (4)$$

First, during the initial magnetizing state, each AlNiCo PM element is set to have a constant  $\mu_r$  and zero  $B_r$ . Then, if a temporary positive magnetizing current is added, the magnetizing force  $H$  of each element can be calculated with TS-FEM. After the initial external magnetizing current is removed, the reversal point will be determined at some specific value. The corresponding remanence of each AlNiCo PM element can be expressed as follows:

$$B_r = \begin{cases} 0 & 0 \leq H \leq H_c \\ \frac{\mu_r \mu_0 H_m + B_{r1}}{H_m - H_c} (H - H_c) - \mu_r \mu_0 H & H_c < H < H_m \\ B_{r1} & H_m \leq H \end{cases} \quad (5)$$

Second, during the working state, the magnetizing force  $H$  of each AlNiCo PM element is calculated with FEM when a temporary negative demagnetizing current is added. Meanwhile,  $B_r$  of each element is obtained based on Equation (2) according to its associated  $B_m$ . Also, at each time step, the value of  $B_m$  is modified until it converges using the under-relax iteration method, which is given by:

$$B_r = \begin{cases} B_m & H_n \leq H \leq 0 \\ \frac{u_r u_0 H_m + B_{r1}}{H_m - H_c} (H + H_c) - u_r u_0 H & -H_c < H < H_n \\ B_m + \mu_r \mu_0 \left[ H + H_c - \frac{(\mu_r \mu_0 H + B_m)(H_m - H_c)}{\mu_r \mu_0 H + B_{r1}} \right] & H \leq -H_c \end{cases} \quad (6)$$

### 3.2. Pole-Pair Regulation

Since the proposed EC-MVSG machine belongs to the magnetic-gearing machine type, its torque transmission is based on the modulation of the airgap flux density distribution along the radial and circumferential directions, therefore, the airgap flux density space harmonics and the corresponding pole-pair arrangements are governed by [7,19,24]:

$$\omega_{a,b} = \frac{ap_{ri}}{|ap_{ri} + bN_{MFS}|} \omega_{ri}, \quad p_{a,b} = |ap_{ri} + bN_{MFS}| \quad (7)$$

where  $a = 1, 3, 5, \dots$ ;  $b = 0, \pm 1, \pm 2, \dots$ ;  $\omega_{ri}$  is the rotating speed of the machine inner rotor;  $p_{ri}$  is the pole-pair number of the machine inner rotor; and  $N_{MFS}$  is the pole-piece number of the MFS. Thus, in order to transmit the torque from the inner rotor to the outer rotor, the outer rotor speed  $\omega_{ro}$  and the pole-pair number  $p_{ro}$  of the outer rotor must be equal to  $\omega_{a,b}$  and  $p_{a,b}$ , respectively. When  $a = 1$  and  $b = -1$ , the largest space harmonic component is attained for torque transmission. Thus, the corresponding airgap flux density space harmonics and the pole-pair number can be rewritten as:

$$\omega_{ro} = \frac{p_{ri}}{|p_{ri} - N_{MFS}|} \omega_{ri}, \quad p_{ro} = |p_{ri} - N_{MFS}| \quad (8)$$

Based on the above equation, the so-called magnetic gearing effect will occur, and the gear ratio and speed relationship can be expressed as:

$$G_r = \frac{p_{ri}}{p_{ro}} \quad (9)$$

$$\omega_{ro} = -G_r \omega_{ri} \quad (10)$$

where the minus sign shows that the two rotors rotate in opposite directions.

For the proposed machine, the MFS is set to 6. The armature winding is set to three phases with six slots also, which can directly locate in the space between MFSs. The pole-pair numbers of both inner rotor and outer rotor are first set to 12. Then, by magnetizing these PMs to the different directions and amplitudes, the proposed machine will have different pole-pair numbers for both rotors. The first case (*Case I*) is to magnetize the inner rotor and outer rotor to the same pole-pair number of four. In this case, both rotors will operate at the same direction, which can be seen as the double-rotor machine. The second case (*Case II*) is to magnetize the inner rotor to the pole-pair of  $p_{ri} = 4$  and  $p_{ro} = 2$ . In this case, the outer rotor speed will be twice as the inner rotor speed with contra-rotating direction. The third case (*Case III*) is to magnetize the inner rotor to the pole-pair of  $p_{ri} = 2$  and  $p_{ro} = 4$ . In this case, the outer rotor speed will be 1/2 as the inner rotor speed with contra-rotating direction. Thus, if the inner rotor speed is set to

500 rpm, the outer rotor speed could be 500 rpm,  $-1000$  rpm or  $-250$  rpm corresponding to the gear ratio of  $G_{r1} = 1$ ,  $G_{r2} = -2$  or  $G_{r3} = -1/2$ .

### 3.3. Electromagnetic Field Analysis

Electromagnetic field analysis has been widely developed for electric machines. Basically, it can be categorized as analytical field calculation and numerical field calculation. The TS-FEM is the one of the most popular numerical field calculation tools. In this paper, the TS-FEM is incorporated with the above parallelogram hysteresis model and developed for analyzing the proposed EC-MVSG machine.

First, the electromagnetic field equation of the machine is governed by [23–25]:

$$\Omega: \frac{\partial}{\partial x} \left( v \frac{\partial A}{\partial x} \right) + \frac{\partial}{\partial y} \left( v \frac{\partial A}{\partial y} \right) = -J - v \left( \frac{\partial B_{ry}}{\partial x} - \frac{\partial B_{rx}}{\partial y} \right) + \sigma \frac{\partial A}{\partial t} \quad (11)$$

where  $\Omega$  is the field solution region;  $A$  is the magnetic vector potential;  $J$  is the current density;  $\sigma$  is the electrical conductivity; and  $B_{rx}$ ,  $B_{ry}$ , are the remanent flux density. It is noted that in each time step, after each magnetization or demagnetization of the AlNiCo PM, the corresponding new remanence is updated by the proposed hysteresis model and then fed into the electromagnetic field equation for computation.

Second, the armature circuit equation of the machine at motoring is given by [25–28]:

$$u_s = R_w i + L_e \frac{di}{dt} + \frac{l_a}{S} \iint_{\Omega_e} \frac{\partial A}{\partial t} d\Omega \quad (12)$$

$$E_a = \frac{l_a}{S} \iint_{\Omega_e} \frac{\partial A}{\partial t} d\Omega = C_e \Phi n \quad (13)$$

where  $u_s$  is the applied voltage;  $R_w$  is the winding resistance;  $i$  is the phase current;  $L_e$  is the end winding inductance;  $l_a$  is the axial length;  $S$  is the conductor area of each phase winding;  $\Omega_e$  is the total cross-sectional area of conductors of each phase winding;  $E_a$  is the armature back EMF;  $C_e$  is the coefficient of flux linkage;  $\Phi$  is the flux linkage; and  $n$  the mechanical rotating speed.

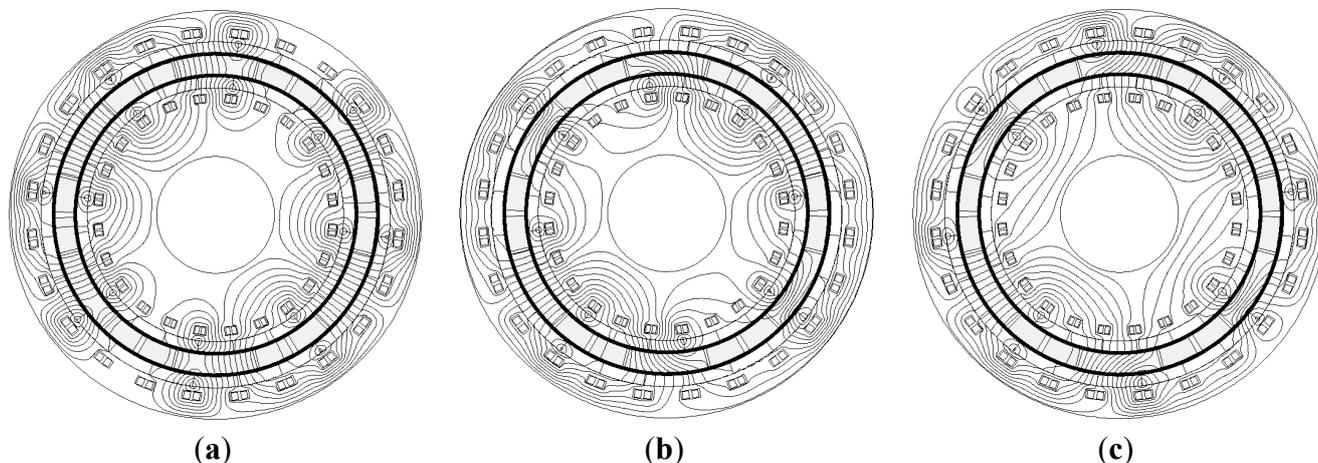
Third, the machine motion equation is expressed as [25–28]:

$$J_m \frac{d\omega_m}{dt} = T_e - T_L - \lambda \omega \quad (14)$$

where  $J_m$  is the moment of inertia;  $\omega_m$  is the mechanical speed;  $T_e$  is the electromagnetic torque;  $T_L$  is the load torque; and  $\lambda$  is the damping coefficient. After discretizing Equations (11)–(14), the TS-FEM can readily be deduced.

Figure 3 shows the flux lines of the proposed machine with different rotor pole-pair numbers and speeds. It can be seen that Figure 3a has four pole-pairs for both rotors, Figure 3b has four pole-pairs for the inner rotor and two pole-pairs for the outer rotor, and Figure 3c has two pole-pairs for the inner rotor and four pole-pairs for the outer rotor. Thus, it proves that the proposed machine can be magnetized to different pole-pair numbers based on the AlNiCo PMs. However, it should be noted that only the indicated pole-pair number is suitable for the proposed machine to work.

**Figure 3.** Flux distribution under inner rotor of 500 rpm: (a) outer rotor speed of 500 rpm with *Case I*; (b) outer rotor speed of 1000 rpm with *Case II*; and (c) outer rotor speed of 250 rpm with *Case III*.



#### 4. Performance Analysis

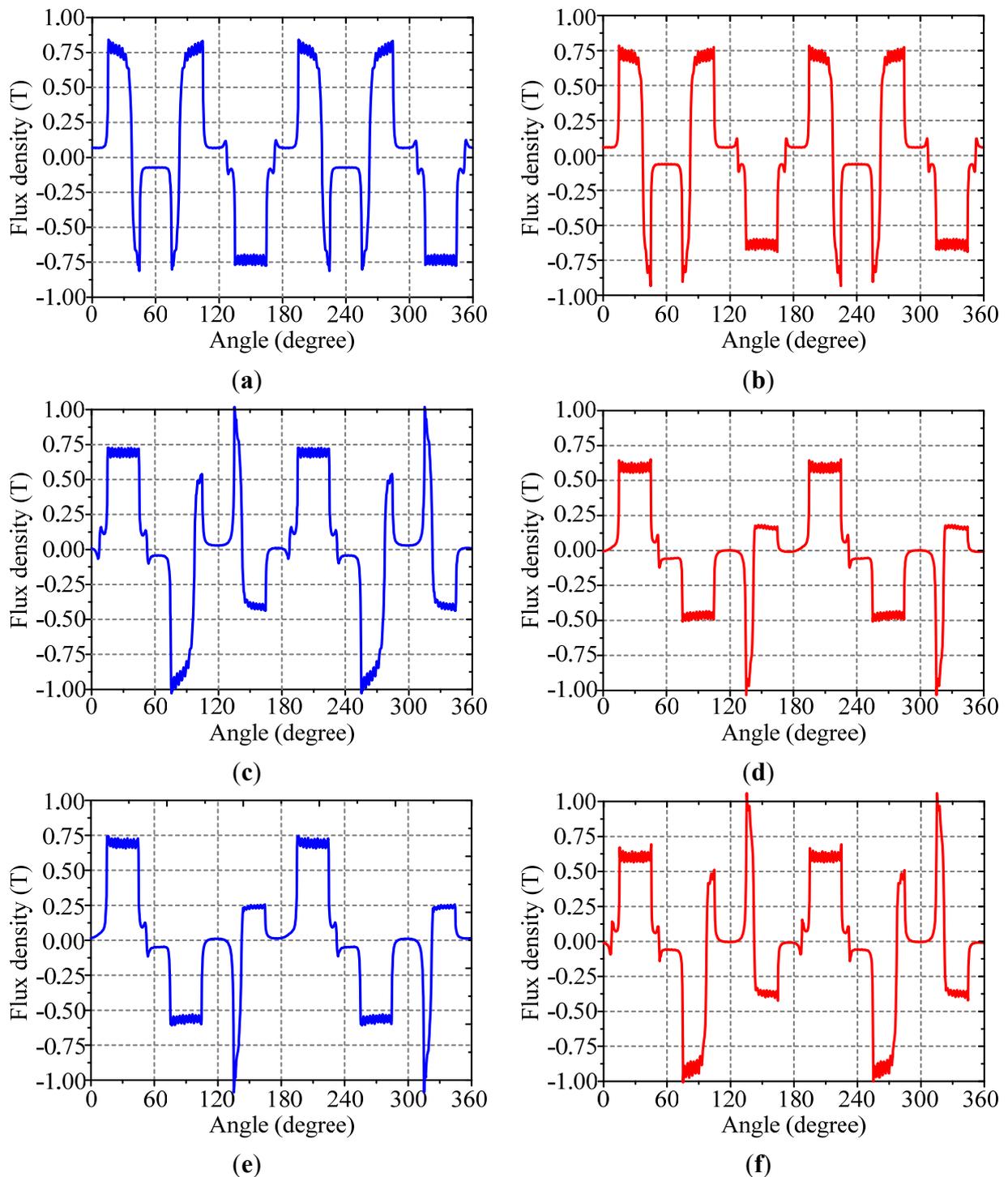
By performing the TS-FEM, the machine performance can be calculated and obtained. The corresponding machine data is listed in Table 1.

**Table 1.** Machine key data. MFSs: modulated ferromagnetic segments.

Item	Value	Item	Value
Outer rotor outside diameter	280.0 mm	Number of MFSs	6
Outer rotor inside diameter	221.2 mm	<i>Case I</i> : number of outer rotor PM pole-pair	4
Inner rotor outside diameter	190.0 mm	<i>Case I</i> : number of inner rotor PM pole-pair	4
Inner rotor inside diameter	80.0 mm	<i>Case II</i> : number of outer rotor PM pole-pair	4
Stator outside diameter	220.0 mm	<i>Case II</i> : number of inner rotor PM pole-pair	2
Stator inside diameter	191.2 mm	<i>Case III</i> : number of outer rotor PM pole-pair	2
Outside airgap length	0.6 mm	<i>Case III</i> : number of inner rotor PM pole-pair	4
Inside airgap length	0.6 mm	Number of phases	3
Shaft length	80.0 mm	Number of stator slots	6
Volume	4,926,017 mm <sup>3</sup>	-	-

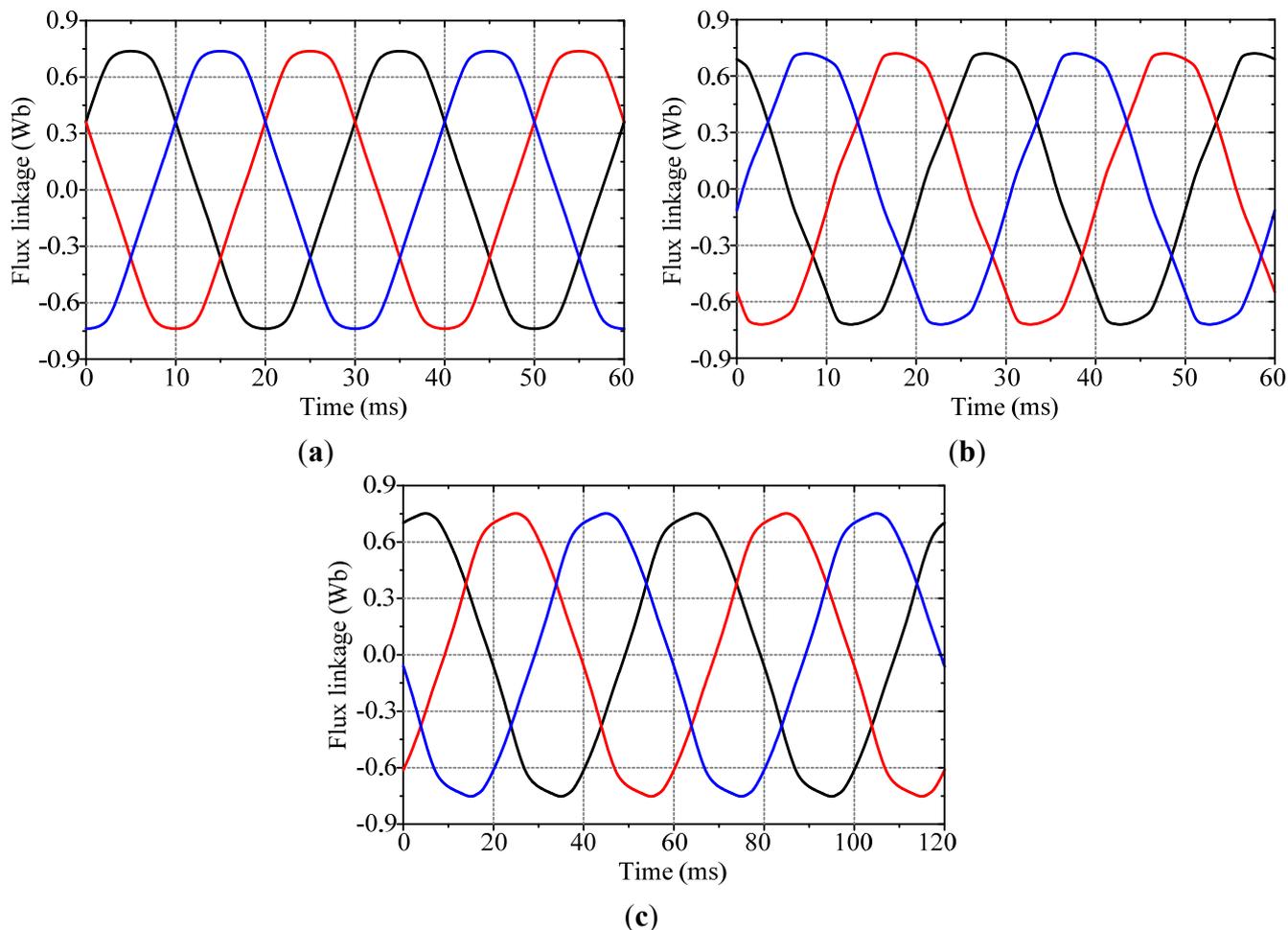
First, the basic characteristics of the proposed EC-MVSG machine are calculated and analyzed. Figure 4 shows the airgap flux density waveforms of the proposed machine under different rotor pole-pair numbers and speeds. It can be found that the amplitude of the airgap flux density is over 0.75 T. Also, they are modulated by the FMSs to different patterns based on different pole-pair numbers. From Figure 4a,b, it can be observed that they have nearly the same flux density waveforms due to the same rotating speed and the same rotor pole-pair numbers. From Figure 4c,d, it can be observed that the outside airgap has been modulated to the small pole-pair number from the big number of the inside airgap. From Figure 4e,f, it can be observed that the outside airgap has been modulated to the big pole-pair number from the small number of the inside airgap. Thus, all these modulation features verify the machine design with EC- MVSG capability.

**Figure 4.** Airgap flux density under different pole-pair numbers: (a) inside airgap with Case I; (b) outside airgap with Case I; (c) inside airgap with Case II; (d) outside airgap with Case II; (e) inside airgap with Case III; and (f) outside airgap with Case III.



Moreover, Figure 5 shows the flux linkages of the proposed machine under different rotor pole-pair numbers. It can be found that the case of both rotors having the same pole-pair number is much more sinusoidal than the other two cases of both rotors having different pole-pair numbers. In addition, due to the modulation effect of MFSSs, the flux linkage periods are different for these three cases for the same inner rotor speed.

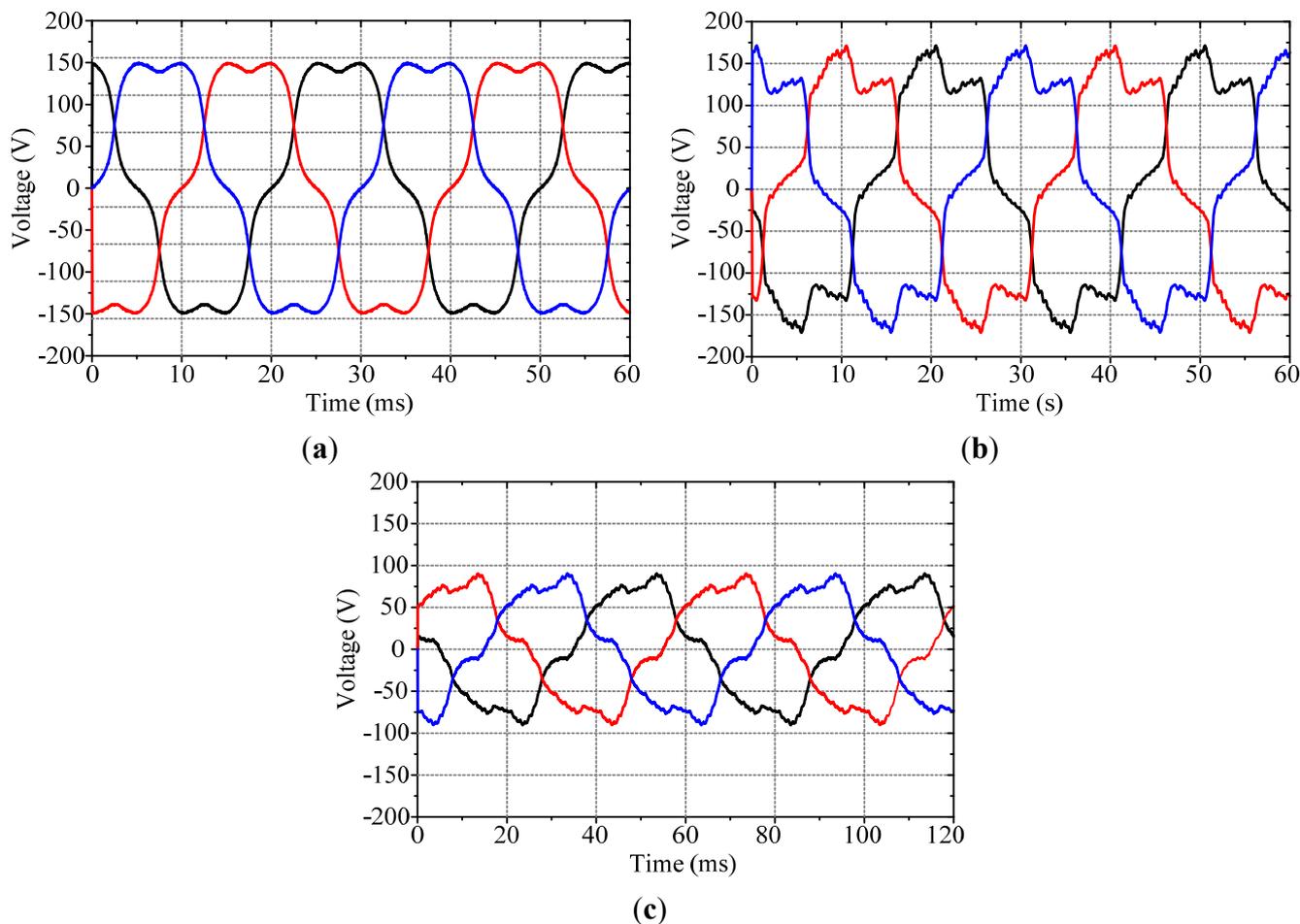
**Figure 5.** Flux linkage waveforms under inner-rotor speed of 500 rpm: (a) with *Case I*; (b) with *Case II*; and (c) with *Case III*.



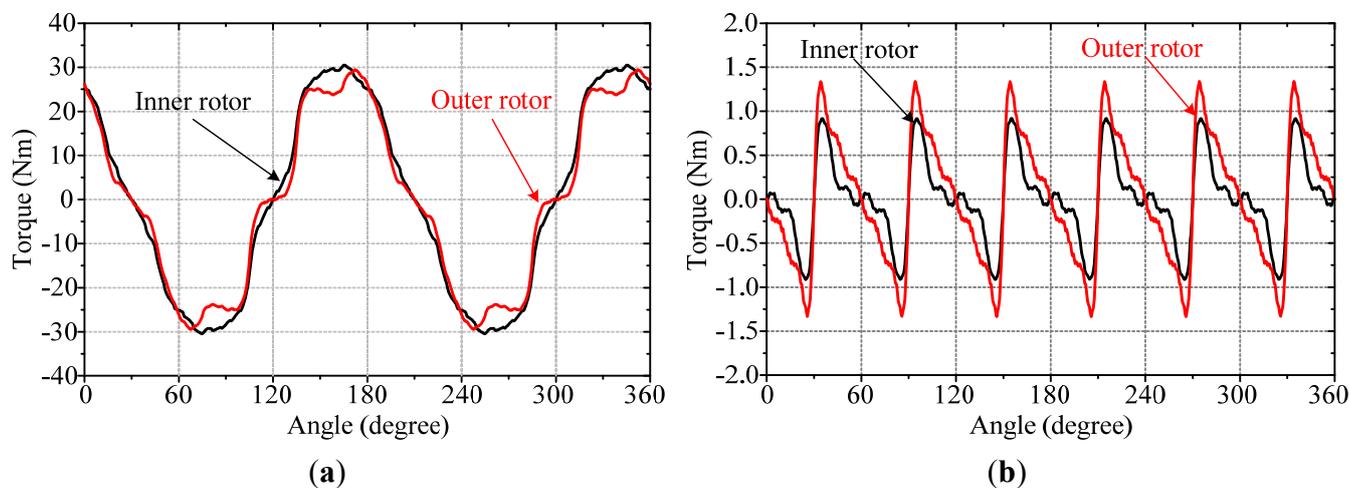
Second, the generating performances of the machine are discussed. Figure 6 shows the no-load EMF waveforms under different rotor pole-pair numbers and speeds. In *Case I*, this machine becomes a double-rotor magnetic-geared machine MGM and produces an EMF value of 150.0 V. In *Case II*, this machine has a raising-speed outer rotor with 1000 rpm and offers a higher EMF value of 171.2 V. In *Case III*, this machine has a decreasing-speed outer rotor with 250 rpm and produces a lower EMF value of 90.2 V. It clearly shows that the proposed machine has three-level gear ratios controlled by the AlNiCo PM magnetization.

Third, the torque performances of the machine are evaluated and discussed. Figures 7–9 show the torque-angle capability and cogging torque of the EC-MVSG machine under the three cases. It should be noted that the torques are generated by feeding the three-phase constant currents of 25 A,  $-12.5$  A and  $-12.5$  A. In *Case I*, it can be found that both inner rotor and outer rotor can produce about the output torque up to 30.0 Nm. This means that the machine can offer in total a maximum torque of 60.0 Nm for driving. In addition, the corresponding cogging torques are both significantly small and below 5% of their inner and rotor output torques. In *Case II*, it can be found that the inner output torque and the outer output torque have contrary directions and maximum values up to 30.0 Nm and 19.2 Nm. This shows that the outer rotor torque reduces the inner rotor torque about 37% by the proposed gearing effect, and hence the outer rotor can run at a high speed, which is twice of that of the inner rotor.

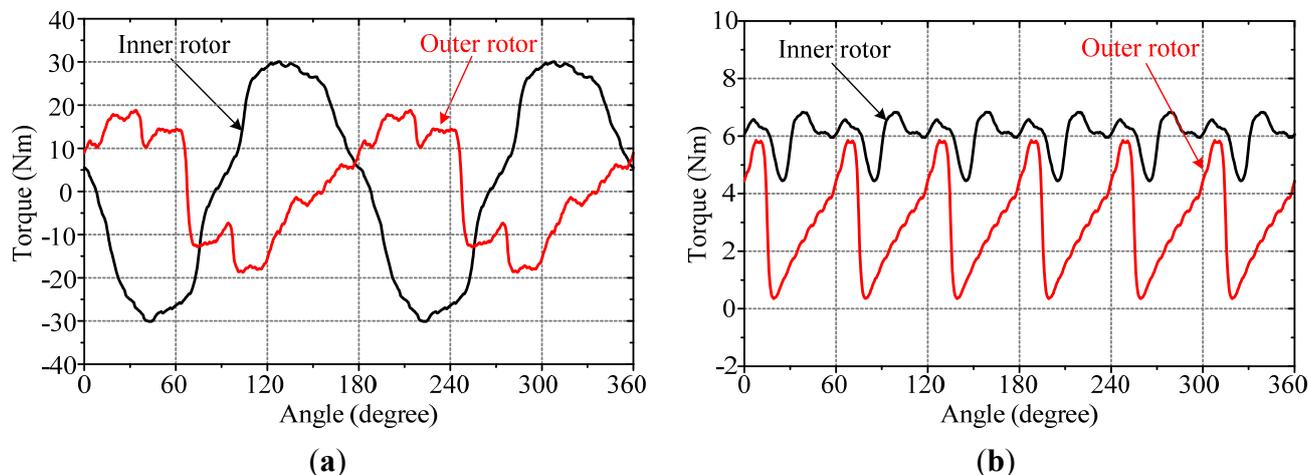
**Figure 6.** No-load EMF waveforms under inner-rotor speed of 500 rpm: (a) outer-rotor speed of 500 rpm with *Case I*; (b) outer-rotor speed of  $-1000$  rpm with *Case II*; and (c) outer-rotor speed of  $-250$  rpm with *Case III*.



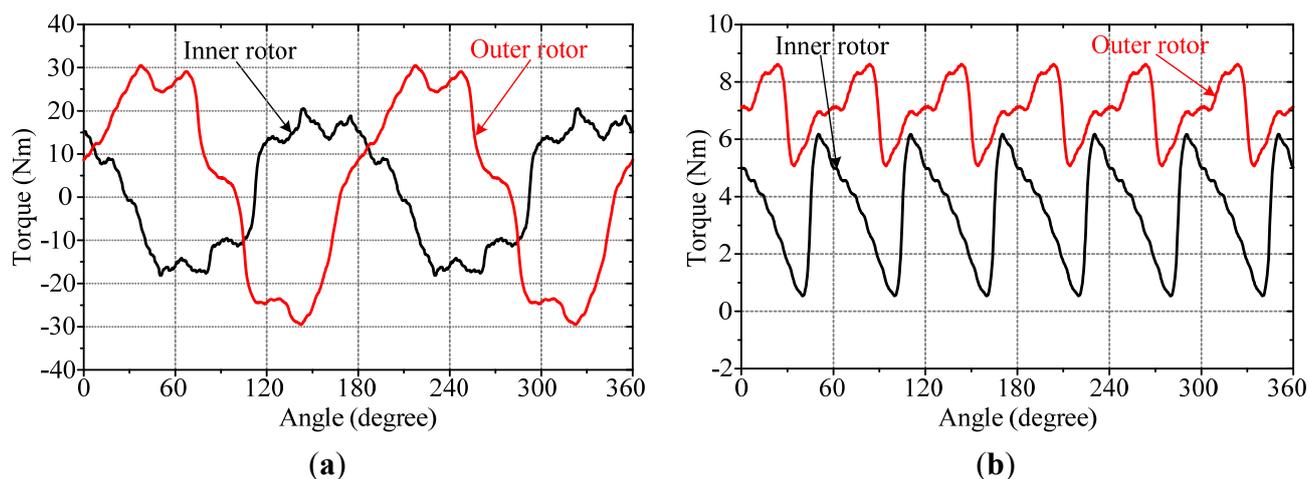
**Figure 7.** Basic torque performances with *Case I*: (a) torque-angle capability; and (b) cogging torque.



**Figure 8.** Basic torque performances with *Case II*: (a) torque-angle capability; and (b) cogging torque.



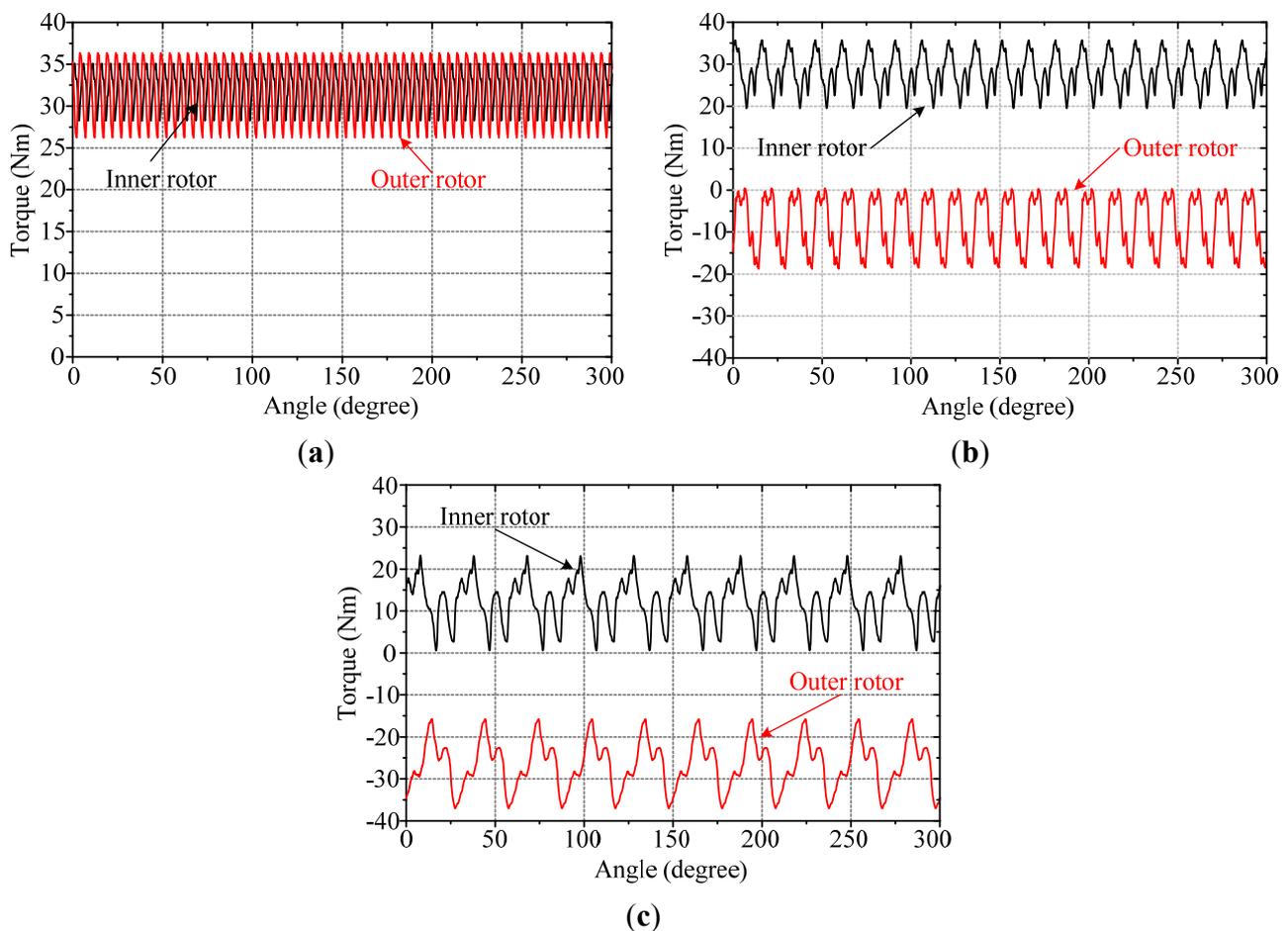
**Figure 9.** Basic torque performances with *Case III*: (a) torque-angle capability; and (b) cogging torque.



In addition, the corresponding cogging torques are not small due to the flux interaction of both rotors, but the cogging torques can be offset to a certain extent. In *Case III*, it can be found that the inner output torque and the outer output torque also have contrary directions and maximum values up to 20.2 Nm and 30.2 Nm. This indicates that the outer rotor torque increases the inner rotor torque by about 50% with the proposed gearing effect, and hence the outer rotor can run at a slow speed, which is only 1/2 of that of the inner rotor. In addition, the cogging torques have a similar effect as those of *Case II*. Since both rotor directions and speeds are different in *Case II* and *Case III*, the corresponding cogging torques are not zero. When the average cogging torque of the outer rotor transfers its energy to the load, the corresponding energy comes from the inner rotor due to their different speeds and directions. It also means that one of the rotors is connected with the external power source, but the total power produced by the two rotor cogging torques is zero. The cogging torques in *Cases II* and *III* are relatively high. Since the two rotors will be connected with the high-inertia engine and high-inertia driveline, respectively, such cogging torques will not significantly affect the engine or vehicle operation.

Moreover, Figure 10 shows the static rated torques of the machine with the same inner rotor speed but different outer rotor speeds. It should be noted that the torques are generated by feeding three-phase sinusoidal currents with an amplitude of 36 A. It can be observed that in *Case I*, the inner rotor and outer rotor can provide average torque outputs of 32.2 Nm and 31.8 Nm. In *Case II*, the inner rotor and outer rotor have static average torques of 28.2 Nm and  $-9.2$  Nm. This means that the outer rotor has a downgraded torque output but with the contrary high-speed operation. In *Case III*, the inner rotor and outer rotor also have contrary torques, which are 12.5 Nm and  $-26.5$  Nm, respectively.

**Figure 10.** Rated torque waveforms under inner-rotor speed of 500 rpm: (a) outer-rotor speed of 500 rpm with *Case I*; (b) outer-rotor speed of  $-1000$  rpm with *Case II*; and (c) outer-rotor speed of  $-250$  rpm with *Case III*.



Finally, Table 2 summarizes the torque performances of the proposed EC-MVSG machine. It shows that in *Case II* and *Case III*, the torque ripples in one rotor are very large, therefore, the rotor with the large torque ripple should operate in a high-inertia or high-power situation, such as the automobile engine. In *Case I*, it indicates that the proposed machine can offer a high torque density of 13 Nm/L which is actually due to the simultaneous contribution of two rotor torques. In *Case II*, the torque density of the outer rotor is quite small (1.87 Nm/L), so that it is mainly used for high-speed occasions. In *Case III*, the machine outer rotor is capable to offer a torque of 5.38 Nm/L for low-speed occasions. *Case I* has a better torque density than the normal PM machine of 10 Nm/L, whereas both *Case II* and *Case III* have lower torque densities.

**Table 2.** Torque performances.

Item	Inner rotor	Outer rotor
Maximum value of torque-angle capability in <i>Case I</i>	30.2 Nm	30.0 Nm
Maximum value of torque-angle capability in <i>Case II</i>	30.0 Nm	19.2 Nm
Maximum value of torque-angle capability in <i>Case III</i>	20.2 Nm	30.2 Nm
Cogging torque in <i>Case I</i>	0.9 Nm	1.3 Nm
Cogging torque in <i>Case II</i>	6.9 Nm	5.9 Nm
Cogging torque in <i>Case III</i>	6.1 Nm	8.8 Nm
Rated torque in <i>Case I</i>	32.2 Nm	31.8 Nm
Rated torque in <i>Case II</i>	28.2 Nm	−9.2 Nm
Rated torque in <i>Case III</i>	12.5 Nm	−26.5 Nm
Torque ripple in <i>Case I</i>	20.4%	30.6%
Torque ripple in <i>Case II</i>	56.2%	208.2%
Torque ripple in <i>Case III</i>	179.8%	79.8%
Torque density in <i>Case I</i>	6.54 kNm/m <sup>3</sup>	6.46 kNm/m <sup>3</sup>
Torque density in <i>Case II</i>	5.73 kNm/m <sup>3</sup>	1.87 kNm/m <sup>3</sup>
Torque density in <i>Case III</i>	2.54 kNm/m <sup>3</sup>	5.38 kNm/m <sup>3</sup>

In addition, the machine's loss and efficiency are calculated and discussed. The copper loss of the machine at rated conditions is 14.4 W. In *Case I*, the iron loss is 56.2 W, and the mechanical loss is assumed to be 94.6 W (3% of the output power). Thus, the machine efficiency in *Case I* is 95.0%. In *Case II*, the iron loss is 74.6 W, and the mechanical loss is assumed to be 30.2 W (3% of the output power). Thus, the machine efficiency in *Case II* is 89.4%. In *Case III*, the iron loss is 44.8 W, and the mechanical loss is assumed to be 47.4 W (3% of the output power). Thus, the machine efficiency in *Case III* is 93.7%. Therefore, it can be found that the proposed machine has an efficiency comparable with other PM machines.

## 5. Conclusions

In this paper, a new type of EC-MVSG machine is presented, which possesses electrically controllable gear ratios for automobile driving. First, the machine structure, design principle, and operation principle are discussed and analyzed in detail. The idea is to change the magnetization of the AlNiCo PM to achieve different rotor pole-pair numbers of the machine. Meanwhile, the machine design adopts the magnetic gearing effect. Thus, the proposed machine not only offers a gearing mechanism for torque and speed transmission, but also provides variable gear ratios for torque and speed variations. Namely, the ratio of the outer-rotor speed to the inner-rotor speed has three values:  $G_{r1} = 1$ ,  $G_{r2} = -2$  and  $G_{r3} = -1/2$ , which means that the machine has three operation cases. In this way, the machine is highly promising for automotive applications. The results demonstrate the effectiveness of the proposed machine design.

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## Conflicts of Interest

The authors declare no conflict of interest.

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