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Published in:
IEEE Access

Published: 01/01/2018

Document Version:
Final Published version, also known as Publisher's PDF, Publisher's Final version or Version of Record

Publication record in CityU Scholars:
Go to record

Published version (DOI):
10.1109/ACCESS.2018.2844400

Publication details:

Citing this paper
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TKSE: Trustworthy Keyword Search Over Encrypted Data With Two-Side Verifiability via Blockchain

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This work was supported in part by the National Key R&D Program of China under Grant 2017YFB0802000, in part by the AXA Research Fund, in part by the National Natural Science Foundation of China under Grants 61772418, 61472472, and 61402366. The work of Y. Zhang was supported by the New Star Team of Xi’an University of Posts and Telecommunications under Grant 2016-02.

ABSTRACT As a very attractive computing paradigm, cloud computing makes it possible for resource-constrained users to enjoy cost-effective and flexible resources of diversity. Considering the untrustworthiness of cloud servers and the data privacy of users, it is necessary to encrypt the data before outsourcing it to the cloud. However, the form of encrypted storage also poses a series of problems, such as: How can users search over the outsourced data? How to realize user-side verifiability of search results to resist malicious cloud servers? How to enable server-side verifiability of outsourced data to check malicious data owners? How to achieve payment fairness between the user and the cloud without introducing any third party? Towards addressing these challenging issues, in this paper, we introduce TKSE, a trustworthy keyword search scheme over encrypted data without any third party, trusted or not. In TKSE, the encrypted data index based on digital signature allows a user to search over the outsourced encrypted data and check whether the search result returned by the cloud fulfills the pre-specified search requirements. In particular, for the first time, TKSE realizes server-side verifiability which protects honest cloud servers from being framed by malicious data owners in the data storage phase. Furthermore, blockchain technologies and hash functions are used to enable payment fairness of search fees without introducing any third party even if the user or the cloud is malicious. Our security analysis and performance evaluation indicate that TKSE is secure and efficient and it is suitable for cloud computing.

INDEX TERMS Blockchain, cloud computing, fair payment, searchable encryption, verifiability.

I. INTRODUCTION

Cloud computing has attracted an increasing number of individuals and organizations to outsource their data to third-party platforms for infinite computing and storage capacity available on demand with inexpensiveness and convenience [1], [2]. Considering the untrustworthiness of cloud servers and the data privacy of users, it is necessary to encrypt the data before outsourcing it to the cloud. However, the direct use of traditional encryption technologies deprives users of search capability and thus results in a poor user experience. In order to preserve the search functionality, searchable encryption technologies have been developed in two representative settings including the symmetric-key setting [3] and the public-key setting [4]. In this paper, we focus on the former, that is, searchable symmetric encryption (SSE), which is usually more practical than the latter in terms of efficiency. However, many important and challenging issues have not been well studied in SSE, such as user-side verifiability and server-side verifiability as illustrated in Figure 1, fair payment, and no trusted third party.

In fact, user-side verifiability takes into consideration that the cloud server may be malicious, that is, the cloud server may only return part of search results or maliciously return incorrect results. The issue of user-side verifiability is firstly
addressed in [5] and [6]. However, these two schemes cannot support server-side verifiability and fair payment without any trusted third party. Furthermore, server-side verifiability takes into consideration that the data owner may be malicious, that is, the data owner may maliciously outsource invalid data in the data storage phase and fraudulently claim compensation later. This concern has not been addressed and even has received little attention in the literature. Last but not least, most of the previous schemes are bank-dependent. Specifically, either the payment issue is not considered or the default traditional payment mechanism is exploited in which a trusted third party (TTP) such as a trustworthy bank has to be introduced for payment fairness. Payment fairness can promote the honest behaviors of users and cloud servers [7]. If a malicious behavior is detected based on the user-side verifiability (resp. server-side verifiability), the data owner (resp. cloud server) should get adequate compensation from the cloud server (resp. data owner) no matter what the cloud server (resp. data owner) does. Therefore, fair payment without any third party is a meaningful and challenging task and it remains in SSE.

In order to thoroughly address the aforementioned challenging issues in cloud computing, we propose TKSE, a Trustworthy Keyword Search scheme over Encrypted data without needing any third party. TKSE is proven secure and our performance evaluation shows its efficiency. In particular, TKSE is characterized by the following desirable features.

- **Keyword Search over Encrypted Data.** The encrypted data index based on the Elliptic Curve Digital Signature Algorithm (ECDSA) allows a user to search over the outsourced encrypted data.
- **User-side Verifiability.** In TKSE, a data owner can embed search requirements into the output script of a joint transaction such that the transaction can be redeemed by the cloud server if and only if the output script evaluates to true based on the returned search result. Therefore, TKSE enables the data owner to resist malicious cloud servers and user-side verifiability is realized.
- **Server-side Verifiability.** Similar to user-side verifiability, the public verification of digital signature enables the cloud server to check the validity of the outsourced encrypted data from the data owner in the data storage phase. Thus, malicious data owners can be detected by the cloud server, which realizes server-side verifiability.
- **Fair Payment and No TTP.** Based on hash functions and ECDSA, TKSE is compatible with blockchains such as the Bitcoin blockchain and the Ethereum blockchain. The global consensus and distributed nature of a blockchain enable a fair payment mechanism in TKSE without introducing any TTP.

The rest of the paper is organized as follows. The related work is discussed in Section II. Some preliminaries are reviewed in Section III. We then formulate problems in Section IV. In Section V, we describe the proposed TKSE scheme in detail. Security analysis and performance evaluation are given in Section VI. Finally, concluding remarks are made in Section VII.

II. RELATED WORK

In recent years, cloud computing technologies have gotten rapid developments and a line of studies have been done on security issues in cloud computing, such as access control [8]–[13] and privacy protection [14]–[19]. As a typical service in cloud computing, cloud storage needs both data security and search functionality. To realize keyword search on remote encrypted data, Song et al. [3] proposed the first searchable encryption scheme in the symmetric setting, in which each keyword is encrypted independently under a two-layer encryption construction. Boneh et al. [4] proposed the first public-key based searchable encryption scheme. Li et al. proposed [20] the first fuzzy keyword search over encrypted data in cloud computing. Curtmola et al. [21] first considered the adaptive security of SSE and presented two index-based schemes. Li et al. [22] proposed a lightweight framework for privacy-aware data queries in cloud computing. However, all the above schemes assume that the cloud server is honest and the returned search result is correct without considering user-side verifiability. In order to resist selfish cloud servers, Kurosawa and Ohtaki [5] first proposed a SSE scheme with user-side verifiability based on [21]. User-side verifiability has also been realized in SSE [6], fuzzy SSE [23], attribute-based keyword search [24], and database update [25], [26]. In these schemes, however, malicious data owners may outsource invalid encrypted data to the cloud server for fraudulent compensation in the future. Similar issues also exist in secure deduplication and data integrity in cloud computing [27]–[29]. Server-side verifiability can be used to tackle this problem but it has not been found in the literature. In addition, all the above schemes are bank-dependent. To be specific, either the payment issue is not taken into account or a TTP is inevitably introduced for fair payment.

To solve the payment fairness issue in cloud computing, blockchain technologies have been taken into account [30], [31]. Andrychowicz et al. [32] proposed secure multiparty lottery protocols based on the Bitcoin blockchain, in which a bitcoin-based timed commitment scheme serves as the main ingredient. In order to realize more general computation, Andrychowicz et al. [33] proposed a two-party computation protocol, which is not compatible with the
Bitcoin blockchain because it modifies the Bitcoin specific-
ification to resist malleability attacks. Similar ideas were
developed independently by Bentov and Kumaresan [34].
Li et al. [35] proposed a blockchain-based SSE scheme,
which requires the miners of the blockchain to do some
particular tasks, such as decryption, and hence violates the
Bitcoin specification. Many other blockchain-based SSE
schemes can be found in [36]–[39], in which the server-side
verifiability remains to be addressed. Besides, blockchain
technologies have also been used in outsourcing com-
putation [40], accountable storage [41] and is combined
with attribute-based signature [42] and homomorphic sig-
nature [43]. It is noticeable that all these schemes are not
compatible with the Bitcoin blockchain, where the scripts are
very limited [44]. For example, the string concatenation is
currently disabled in Bitcoin scripts.

III. PRELIMINARIES

A. NOTATIONS

In Table 1, we summarize important notations used in TKSE
for ease of reference.

<table>
<thead>
<tr>
<th>Notation</th>
<th>Meaning</th>
</tr>
</thead>
<tbody>
<tr>
<td>User</td>
<td>The data owner and consumer, a.k.a. the user.</td>
</tr>
<tr>
<td>CSP</td>
<td>The cloud service provider.</td>
</tr>
<tr>
<td>$x \in \mathbb{R}$</td>
<td>An element $x$ is randomly chosen from the set $\mathbb{R}$.</td>
</tr>
<tr>
<td>$N$</td>
<td>The number of documents.</td>
</tr>
<tr>
<td>$[m]$</td>
<td>The set ${i \in \mathbb{Z}^+</td>
</tr>
<tr>
<td>$r_p$</td>
<td>A secret of the cloud service provider.</td>
</tr>
<tr>
<td>$h_{\sigma}$</td>
<td>The hash value $H(r_p)$, where $H$ is a hash function.</td>
</tr>
<tr>
<td>$t$</td>
<td>A time-lock.</td>
</tr>
<tr>
<td>$T$</td>
<td>A data tree.</td>
</tr>
<tr>
<td>$\ell$</td>
<td>The height of $T$.</td>
</tr>
<tr>
<td>$\mathcal{D}$</td>
<td>A set of documents $\mathcal{D} = {D_i}_{i \in [N]}$.</td>
</tr>
<tr>
<td>$\mathcal{C}$</td>
<td>The ciphertext data set of $\mathcal{D}$ and $\mathcal{C} = {C_i}_{i \in [N]}$.</td>
</tr>
<tr>
<td>$\mathcal{I}$</td>
<td>The index set with respect to $\mathcal{D}$.</td>
</tr>
<tr>
<td>$\mathcal{W}$</td>
<td>A set of keywords with respect to $\mathcal{D}$.</td>
</tr>
<tr>
<td>$\mathcal{D}_{\omega}$</td>
<td>The set of documents which contain a keyword $\omega \in \mathcal{W}$.</td>
</tr>
<tr>
<td>$\mathcal{C}_{\omega}$</td>
<td>The ciphertext data set of $\mathcal{D}_{\omega}$.</td>
</tr>
<tr>
<td>$(pk_A, sk_A)$</td>
<td>An ECDSA public and secret key pair of $A$.</td>
</tr>
<tr>
<td>$\sigma_{\text{com}}$</td>
<td>The ECDSA signature of the root of $T$.</td>
</tr>
<tr>
<td>$\max B$</td>
<td>The maximal delay between broadcasting a transaction and including it on the blockchain.</td>
</tr>
</tbody>
</table>

B. BLOCKCHAIN

As an essential technology behind Bitcoin [30] and Ether-
ereum [31], the idea of blockchain is that the longest
chain is accepted as the proper one. In TKSE, the bitcoin-
based timed commitment scheme [32] is used to resist mali-
icious behaviors, which is also adopted by [40] and [41].
The commitment scheme is denoted by CS(Commit, User, CSP, $d, t, s$)
and is executed between User and CSP. Here, User and
CSP represent the user and the cloud service provider
in TKSE. They act as the committer and the receipt in
the commitment scheme, respectively. Concretely, CSP
commits to a secret $s$ and has to open the commitment
before a specific time $t$ to get his/her deposit of value
$d \mathcal{B}$ back. Otherwise, the deposit will be redeemed by
User. The commitment scheme consists of three phases: the
commitment phase CS.Commit(CSP, User, $d, t, s$), the
opening phase CS.Open(CSP, User, $d, t, s$) and the pun-
ishment phase CS.Fine(CSP, User, $d, t, s$). Note that the
punishment phase is performed only if the opening phase
is not correctly performed. Please refer to [32] for more
details.

C. SPECIFICATION OF TWO-SIDE VERIFIABLE SSE

A two-side V-SSE scheme is composed of seven polynomial
time algorithms (KeyGen, Encrypt, BuildIndex, Trapdoor,
Search, Verify, Decrypt) as below. The specification is the
same as the one given in [5] except that index generation is
separated from data encryption for clarity and the index is
publicly verifiable.

- **KeyGen($1^k$) → $K$:** Given a security parameter, it outputs
  a secret key $K$.
- **Encrypt($K, D$) → $C$:** Given $K$, a document set $D$, it outputs a ciphertext data set $C$.
- **BuildIndex($K, D, C, W$) → $I$:** Given $K, D, C$ and a keyword set $W$, it outputs an index set $I$. Note that $C$ and $W$ can be generated based on $K$ and $D$. We explicitly take them as inputs for the simplicity of exposition.
- **Trapdoor($K, \omega$) → $T_\omega$:** Given $K$ and a keyword $\omega$, it outputs a trapdoor $T_\omega$ associated with $\omega$.
- **Search($I, C, T_\omega$) → ($C_\omega, tag_\omega$):** Given $I, C$ and $T_\omega$, it outputs a ciphertext data set $C_\omega$ and a tag set $tag_\omega$ associated with $\omega$.
- **Verify($T_\omega, C_\omega, tag_\omega$) → 1 or 0:** Given $T_\omega, C_\omega$ and $tag_\omega$, it outputs 1 if the search result is valid and 0 otherwise.
- **Decrypt($K, C$) → $D$:** Given $K, C$, it outputs $D$.

In Section V, the design of TKSE is described in detail. We will see that an underlying two-side V-SSE scheme is used in
TKSE, in which KeyGen, Encrypt and Decrypt are based on
a symmetric encryption algorithm, and verifiable BuildIndex
is based on a digital signature.

IV. PROBLEM FORMULATION

A. SYSTEM MODEL

As shown in Figure 2, the entities involved in TKSE include
a data owner, a data consumer, a cloud service provider
(i.e., CSP) and a blockchain. In TKSE, we focus on search-
able symmetric encryption. In other words, the data owner
and the data consumer are essentially the same entity (i.e.,
User) because they share a secret key. Suppose User intends
to outsource some documents to CSP while keeping data
confidentiality, searching ability and verifiability. The main
procedures are presented in Figure 2. Obviously, TKSE
consists of three phases including data storage phase, data
search phase and user claim phase. In the data storage
phase, User generates encrypted data and index by pro-
cedure (1) and outsourcing them to CSP. Based on pro-
cedure (2), data storage is enforced by CSP after ensur-
ing its validness. Procedures (3.1) and (3.2) are used by
User to confirm the enforcement of data storage. On the
other hand, data search is enabled by procedures (4), (5.1),

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FIGURE 2. The system model of TKSE. (a) Data Storage Phase. (b) Data Search and User Claim Phase.

(5.2), (6), (7.1) and (7.2). The search request is based on procedure (4) and the search commitment is realized in procedures (5.1) and (5.2). The payment commitment is based on procedure (6). Procedures (7.1) and (7.2) are used to realize verification and payment. Finally, procedure (8) allows User to claim compensation due to search payment if the search result is invalid in the data search phase. In TKSE, a public blockchain is considered, such as the Bitcoin blockchain and the Ethereum blockchain.

B. ADVERSARY MODEL AND DESIGN GOALS

In TKSE, both User and CSP can be malicious and they are of mutual distrust. Specifically, the following malicious behaviors should be taken into consideration.

- **Case 1.** Malicious CSP may try to learn information on secret keys and original documents of User from trapdoor and ciphertext data.
- **Case 2.** Malicious CSP may forge search results or return partial results.
- **Case 3.** Malicious User may defraud CSP for compensation by outsourcing invalid ciphertext data and index to CSP in the data storage phase.
- **Case 4.** Malicious CSP aims to obtain search fees from User without providing search results satisfying the requirements of User.
- **Case 5.** Malicious User wants to get valid search results from CSP without paying the search fee.

Considering the above attacks, the design goals of TKSE are as follows.\(^1\)

- **Privacy.** In TKSE, it is impossible for CSP to learn any information on secret keys and original documents. This goal is against the attack in Case 1.
- **User-side Verifiability.** It is the same as the property reliability in [5]. This goal is against the attack in Case 2. That is, CSP cannot forge valid search results or return partial results.
- **Server-side Verifiability.** This goal is against the attack in Case 3 and it can protect CSP from being framed by malicious User.
- **Fair Payment.** This goal is against attacks in Case 4 and Case 5. Specifically, fairness ensures that User can get valid search results only if corresponding search fees are paid to CSP. On the other hand, CSP obtains search fees from User only if satisfactory search results are returned.

In addition, considering that blockchain technologies are used in TKSE, the following attractive properties should be achieved.

- **No TTP.** It means that payment fairness is realized without introducing any TTP.
- **Compatibility.** TKSE should be compatible with mainstream blockchains such as Bitcoin and Ethereum. Note that if TKSE is compatible with the Bitcoin blockchain, then it is compatible with Ethereum blockchains [44], [45].

C. DEFINITION OF TKSE

TKSE is composed of four phases including the initialization phase, the data storage phase, the data search phase and the user claim phase. The first three phases are compulsory and the user claim phase is performed by User when CSP is malicious. The definition of TKSE is as follows.

1) **INITIALIZATION**

User and CSP initialize parameters to be used in the subsequent phases, such as their own secret keys and unredeemed transactions on the blockchain.

\(^1\) As shown in Section VI, TKSE achieves privacy and user-side verifiability in the universal composability framework similar to [5].
2) DATA STORAGE PHASE
The outsourcing of data storage is implemented in this phase. Four procedures, data encryption, index generation, storage enforcement and storage confirmation, are sequentially performed as follows.

- **Data Encryption**: For confidentiality, User encrypts $D$ to get $C$ which is outsourced to CSP.
- **Index Generation**: User generates $I$ and sends it together with $C$ to CSP.
- **Storage Enforcement**: CSP firstly checks and stores $I$ and $C$. Then, CSP generates a digital signature according to $C$ and stores the signature on the blockchain. Finally, CSP sends such information to User that helps User to get the signature from the blockchain.
- **Storage Confirmation**: Upon getting the signature from the blockchain, User thinks that $C$ has been stored by CSP.

3) DATA SEARCH PHASE
In this phase, CSP searches his/her storage according to the requirements of User. It can be ensured that CSP earns search fees from User if and only if User obtains valid search results. Four sequential sub-phases are performed, including search request, search commitment, payment commitment, and verification and payment.

- **Search Request**: User generates a search request based on $W$ and sends it to CSP. Besides, the compensation and penalty of CSP in the case of invalid search should be specified by User and CSP.
- **Search Commitment**: This phase is used by CSP to commit to that if search results cannot meet the requirements specified in Search Request and malicious CSP refuses to compensate User in the subsequent phase Verification and Payment before a given time, User is able to claim enough deposits of CSP by himself/herself as a penalty in the subsequent User Claim Phase after the given time.
- **Payment Commitment**: User commits to CSP that if the search result is valid, CSP is able to earn search fees in Verification and Payment. It is realized by temporarily freezing a deposit consists of service fee from User, in which the search requirements are specified.
- **Verification and Payment**: To demonstrate that he/she agrees with the search requirements of User, CSP further freezes a deposit consists of his/her guaranty. Then, CSP earns the service fee of User by providing search results and proving that the search result meets the requirements of User. Finally, User gets search results from the proof of CSP and decrypts them to obtain original documents.

4) USER CLAIM PHASE
Only if CSP fails to prove that the search result meets the requirements of User before the given time, TKSE comes to User Claim Phase. It is used by User to claim enough deposits of CSP no matter how CSP behaves.

V. TRUSTWORTHY SEARCH OVER ENCRYPTED DATA
In this section, we first give an overview of TKSE, and then describe its design in detail.

A. HIGH LEVEL DESCRIPTION
In TKSE, privacy is realized similar to the SSE scheme [5]. The scheme [5] realizes user-side verifiability by designing indexes based on a message authentication code (MAC) with a secret key. Because the MAC secret key is only known by User, the server-side verifiability cannot be achieved in [5]. Furthermore, the idea in [5] cannot be directly combined with Blockchain technologies in that the condition of redeeming search fees should be specified by User and CSP and it requires the MAC secret key. If CSP gets the secret key, he/she can generate “search results” arbitrarily and ensure they can pass the user-side verifiability, which violates payment fairness. In TKSE, we build the index based on a signature scheme and hash functions instead of MAC. In this case, although CSP is able to publicly check the search results, he/she cannot forge valid search results arbitrarily because of the unforgeability of the digital signature and the collision-resistance of hash functions. In order to eliminate TTP and realize compatibility with typical blockchains especially the Bitcoin blockchain, we exploit ECDSA in TKSE.

B. DESIGN DETAILS OF TKSE
1) INITIALIZATION
Let $\pi_0$ be a pseudo-random permutation,

$$
\pi_0 : \{0,1\}^\lambda \times \{0,1\}^{1+\ell_w+\ell} \rightarrow \{0,1\}^{1+\ell_w+\ell},
$$

where $\lambda$ is a security parameter, $\ell_w$ is the bit length of a keyword, and $\ell$ represents the bit length of a document with $N = 2^\ell$. User chooses $K_0 \in \{0,1\}^\lambda$ as a key of $\pi_0$ and defines $\pi(\cdot) = \pi_0(K_0, \cdot)$. In addition, User chooses a secure cryptographic hash function $H$ and a symmetric encryption scheme with functions

$$(\text{KeyGen}_\text{SE}, \text{Encrypt}_\text{SE}, \text{Decrypt}_\text{SE}),$$

and sets $K_{\text{SE}} = \text{KeyGen}_\text{SE}(1^\lambda)$. Finally, we assume User and CSP choose their own ECDSA public and secret key pairs, denoted by $(pk_U, sk_U)$ and $(pk_S, sk_S)$, respectively. CSP prepares an unredeemed transaction $\text{Tx}_{\text{Sig}}^3$ of value $d_{\text{sig}} \mathbb{B}$, which can be redeemed with $sk_S$. User sets $K = (K_0, K_{\text{SE}}, sk_U)$ as his/her secret key.

2) DATA STORAGE PHASE
The outsourcing of $D$ is implemented based on the following four procedures.
Algorithm 1 BuildIndex($K, D, C, W$) → $I$

**Input**: secret key $K$, document set $D$, ciphertext data set $C$, keyword set $W$

**Output**: index $I$

1. for $i ∈ [\text{num}]$ do
2.   $I(i) = (\text{dummy}, \sigma_{I}(i \parallel H(\text{dummy})))$
3. end
4. for $ω ∈ W$ do
5.   Suppose $D_0 = \{D_{s1}, D_{s2}, \ldots, D_{num}\}$.
6.   for $j ∈ [\text{num}]$ do
7.     $\text{addr}_{ω,j} = \pi(0, ω, j)$
8.     $\text{tag}_{ω,j} = \sigma_{I}(\text{addr}_{ω,j} \parallel H(C_j))$
9.     $I(\text{addr}_{ω,j}) = (j, \text{tag}_{ω,j})$
10. end
11. end
12. for $k ∈ D$ do
13.   Suppose $k$ has already appeared $N_k$ times in $I$.
14.   if $N_k ≠ 2^{ℓω}$ then
15.     for $1 ≤ r ≤ 2^{ℓω} − N_k$ do
16.       $\text{addr}_{r,k} = \pi(1, r, k)$
17.       $\text{tag}_{r,k} = \sigma_{I}(\text{addr}_{r,k} \parallel H(C_k))$
18.       $I(\text{addr}_{r,k}) = (k, \text{tag}_{r,k})$
19.     end
20. end
21. end
22. return $I$

- **Data Encryption**: For $i ∈ [N]$, User computes $C_i = \text{Encrypt}_SE(K_{SE}, D_i)$. Then $C = \{C_i\}_{i=1}^N$ will be outsourced to CSP.

- **Index Generation**: User generates $I$ based on BuildIndex as shown in Algorithm 1 and sends $I$ together with $C$ to CSP, where $I$ is an array of size $2^{1+4ω+3\text{num}}$.

- **Storage Enforcement**: CSP stores $I$ and $C$ after ensuring the validity based on signature verification. Furthermore, to earn search fees of User in the subsequent phases, a Merkle tree $T$ is built by CSP, where the leaf nodes consist of $C$. An example of $N = 8$ is shown in Figure 3, where

$$h_i = H(C_i), h_{i,j} = H(h_i \parallel h_j)$$

and $I_{\text{root}} = H(h_{1-4} \parallel h_{5-8})$ with $h_{1-4} = H(h_{1,2} \parallel h_{3,4})$ and $h_{5-8} = H(h_{5,6} \parallel h_{7,8})$. Furthermore, CSP computes $\sigma_{\text{root}} = \sigma_{G}(I_{\text{root}})$, and stores $\sigma_{\text{root}}$ on the blockchain by broadcasting a search signature transaction $TxSearchSig$, as illustrated in Figure 4. Finally, CSP sends the transaction ID to User.

- **Storage Confirmation**: Upon receiving the transaction ID from CSP, User first gets $\sigma_{\text{root}}$ from the blockchain. Then, User computes $I_{\text{root}}$ based on $C$. If $\text{ver}_S(I_{\text{root}}, \sigma_{\text{root}}) = \text{true}$, User thinks $C$ has been stored by CSP. User deletes $D$, $C$ and just stores $ℓ$ and the transaction ID as metadata.

3) **DATA SEARCH PHASE**

It is introduced based on the following four procedures.

- **Search Request**: Suppose User wants to search documents with a keyword $ω ∈ W$, he/she generates a trapdoor $T_ω$, based on $\text{Trapdoor}$ as below and sends $T_ω$ to CSP. Note that $T_ω$ is used as a search request.

$\text{Trapdoor}(K, ω) → T_ω$: Taking the secret key $K$ and a keyword $ω$ as inputs, User outputs $T_ω = (\pi(0, ω, 1), \pi(0, ω, 2), \ldots, \pi(0, ω, N))$.

Besides, CSP prepares an unredeemed transaction $Tx_{0}^S$ of value $d_{0}^B$, which can be redeemed by $sk_S$ and is used as his/her penalty in the case of invalid search. Furthermore, suppose there are unredeemed transactions $Tx_{0}^U$ of value $d_{1}^U$ and $Tx_{0}^B$ of value $d_{1}^B$, which can be redeemed by User and CSP, respectively. In order to force CSP to compensate User before a specific time once the search is invalid, let $d_{0} ≥ d_{1}^U + d_{1}^B$. Note that, $d_{1}^U$ and $d_{1}^B$ denote the search fee of User and the compensation of CSP in the case of search failure, respectively.

- **Search Commitment**: Upon receiving $T_ω$, CSP performs $\text{CS.Commit}(\text{CSP}, \text{User}, d_0, t, r_s)$, where $r_s ∈ R$.
\(0, 1\)\(^*\). Specifically, CSP posts a deposit transaction \(\text{TxSearchCommit}\) of value \(d_0\) \(\mathbb{B}\) on the blockchain, which commits to that once the search result cannot meet the requirements specified in Search Request and malicious CSP refuses to compensate User in Verification and Payment before time \(t\). User is able to claim enough deposits of CSP by himself/herself as a penalty in the subsequent User Claim Phase after time \(t\). The details of \(\text{TxSearchCommit}\) are shown in Figure 5, where \(h_S = H(r_S)\).

Once \(\text{TxSearchCommit}\) is included on the blockchain, CSP creates the body of the punishment transaction \(\text{TxFine}\), which will be used by User to claim the penalty, signs it and sends the signed body \(\text{sig}_3(\text{TxFine})\) to User. \(\text{TxOpen}\) and \(\text{TxFine}\) will be detailed in Verification and Payment and User Claim Phase, respectively. Certainly, if the search is valid, CSP will eventually get the deposit back no matter how User behaves. In particular, CSP performs the search algorithm Search described in Algorithm 2 to obtain \(C_o\) and \(\text{tag}_o\). Suppose \(C_o = \{C_j\}_{j \in I_o}\). CSP sets \(H_o = \{H(C_j)\}_{j \in I_o}\) and \(\text{path}_o = H_o \cup \mathbb{A}_o\), where \(\mathbb{A}_o\) represents the set of auxiliary node values of \(H_o\) in \(T\). Take the case of \(N = 8\) and \(C_o = \{C_1, C_6\}\) as an example, as shown in Figure 3. We know \(H_o = \{h_1, h_6\}\) and \(\mathbb{A}_o = \{h_2, h_5, h_3, h_4, h_7, h_8\}\). It’s noted that the root value can be easily recovered based on \(\text{path}_o\), which is sent to User by CSP.

**Payment Commitment:** Once \(\text{TxSearchCommit}\) is included on the blockchain, and \(\text{sig}_3(\text{TxSearch})\) are received, User makes a payment commitment that CSP is able to get corresponding search fee if the search result is valid in Verification and Payment. In fact, User performs the following procedures:

\begin{algorithm}
\caption{Search(\(I, C, T_o\)) \(\rightarrow\) \(\{C_o, \text{tag}_o\}\)}
\begin{algorithmic}[1]
\Require index \(I\), ciphertext data set \(C\), trapdoor \(T_o\)
\Ensure ciphertext data set \(C_o\) and tag set \(\text{tag}_o\) with respect to \(o\)
\begin{algorithmic}
\State Let \(C_o = \emptyset\).
\State Parse \(T_o = (\text{addr}_{o,1}, \text{addr}_{o,2}, \ldots, \text{addr}_{o,N})\).
\For{\(j \in [N]\)}
\State \(I(\text{addr}_{o,j}) = (s_j, \text{tag}_{o,j})\)
\If{\(s_j \neq \text{dummy}\)}
\State set \(C_o = C_o \cup C_j\)
\EndIf
\EndFor
\State Set \(\text{tag}_o = (\text{tag}_{o,1}, \text{tag}_{o,2}, \ldots, \text{tag}_{o,N})\).
\State return \(C_o\) and \(\text{tag}_o\)
\end{algorithmic}
\end{algorithm}
\end{algorithm}

- Compute \(I_{\text{root}}\) based on \(\text{path}_o\).
- Parse \(\text{path}_o = H_o \cup \mathbb{A}_o\) and \(H_o = \{H(C_j)\}_{j \in I_o}\).
- Check if \(\text{vers}(I_{\text{root}}, \sigma_{\text{root}}) = \text{true}\), where \(\sigma_{\text{root}}\) can be obtained from the blockchain based on metadata. If it is, User proceeds. Otherwise, User quits.
- Define \(h_j = H(C_j)\) for \(j \in I_o\) and \(h_{\text{dummy}} = H(\text{dummy})\) for \(j \in [N] - I_o\).
- Set \(M_o = (m_{o,j})_{j \in [N]}\), where \(m_{o,j} = \text{addr}_{o,j} \| h_j\).
- Choose single variable \(x\) and two variable sets \(\text{chal}_1\) and \(\text{chal}_2\), where
\[
\text{chal}_1 = \{c_{1,j}\}_{j \in I_o}, \quad \text{chal}_2 = \{c_{2,j}\}_{j \in [N]}.
\]
- Create the body of the joint deposit transaction \(\text{TxVeriPay}\), as illustrated in Figure 7, signs it and sends the signed body \(\text{sig}_2(\text{TxVeriPay})\) to CSP. In Figure 7, \(\text{check}_1\) and \(\text{check}_2\) are defined as
by immediately putting the refund to and the CSP.

4) USER CLAIM PHASE
Suppose CSP fails to prove that the search result meets the requirements of User before time \(t - 2 \max B\), TKSE comes to User Claim Phase. It is used by User to claim enough deposits of CSP no matter how CSP behaves. We consider the following two cases.

- Case 1. CSP refuses to pay the compensation \(d^2 \mathcal{B}\) to User. User performs CS.Fine(CSP, User, \(d_0, t, r_s\)), in which User gets the penalty \(d_0 \mathcal{B}\) by posting the punishment transaction TxFine on the blockchain, and then quits. The detail of TxFine is given in Figure 8.

- Case 2. CSP refuses to pay the penalty \(d_0 \mathcal{B}\) to User. User gets both the refund \(d^1 \mathcal{B}\) and the compensation \(d^2 \mathcal{B}\) by immediately putting the refund transaction TxRefund and the compensation transaction TxCompensation on the blockchain, respectively. Then User quits. TxRefund and TxCompensation are explained in Figure 7.

VI. SECURITY, COMPATIBILITY AND PERFORMANCE ANALYSIS
A. SECURITY ANALYSIS AND COMPATIBILITY
TKSE is secure based on Theorem 1, Theorem 3 and Theorem 2 and it achieves compatibility based on Theorem 4.

Theorem 1 (Privacy and User-Side Verifiability): TKSE satisfies privacy and user-side verifiability if the adopted hash function \(H\) is collision-resistant, the symmetric key encryption scheme has left-or-right indistinguishability as defined by [46] and the ECDSA signature is unforgeable under chosen message attacks.

Proof: We know from Section V that an underlying V-SSE scheme is used in TKSE. In particular, V-SSE is designed based on [5] and [21]. Specifically, based on the SSE scheme [21], the scheme [5] further realizes verification of search results by designing indexes based on MAC with a secret key. In V-SSE, we generate indexes based on \(H\) and ECDSA. Therefore, if \(H\) is collision-resistant, it directly follows from the unforgeability of ECDSA signature and MAC that V-SSE has the same security as [5]. Based on the security of [5], we know that TKSE satisfies privacy and user-side verifiability as described in Theorem 1.
Theorem 2 (Server-Side Verifiability): TKSE satisfies server-side verifiability if the adopted hash function $H$ is collision-resistant and the ECDSA signature is unforgeable under chosen message attacks.

Proof: In the data storage phase of TKSE, after receiving ciphertext data set $C$ and index $I$ from User, CSP firstly performs ECDSA verification to ensure the validity of $C$ and index $I$. Then, the storage enforcement procedure is performed by CSP. Therefore, if $H$ is collision-resistant, it directly follows from the public verifiability and unforgeability of the ECDSA signature that TKSE satisfies server-side verifiability.

Theorem 3 (Fair Payment and No TTP): TKSE realizes fair payment without needing any TTP if the adopted hash function $H$ is collision-resistant and the ECDSA signature is unforgeable under chosen message attacks.

Proof: In TKSE, public blockchains are introduced. Therefore, eavesdropping attacks may be made by a malicious party to undermine the fairness of the honest party. In the following, we consider two cases.

Suppose User is honest and CSP is malicious. In this case, CSP wants to obtain search fees from User without returning a valid search result satisfying the requirements of User before time $t - 2 \times \text{max}_B$. At the same time, CSP cannot pay compensation or penalty to User. If User does not get a valid search result, the joint deposit transaction $\text{TxVeriPay}$ cannot be redeemed by CSP based on $\text{TxSearchFee}$ and $\text{TxGuaranty}$ before time $t - 2 \times \text{max}_B$ in the verification and payment phase. According to the definitions of $\text{check}_1$, $\text{check}_2$ in the payment commitment phase and $\text{SearchResult}_1$, $\text{SearchResult}_2$ in the verification and payment phase, we know CSP cannot obtain the search fee $d^C_B$ from User unless CSP is able to forge an ECDSA signature or find a collision of the hash function $H$. To be specific, if CSP refuses to pay the compensation $d^S_B$ to User, which means CSP does not open the search commitment by broadcasting $\text{TxOpen}$ based on $\text{CS.Open}$ before time $t$, User performs $\text{CS.Fine}$, in which User obtains the penalty $d_0B$ with $d_0 \geq d^C + d^S$ by posting the punishment transaction $\text{TxFine}$ on the blockchain. On the other hand, if CSP refuses to pay the penalty to User, which means CSP opens the search commitment by performing $\text{CS.Open}$ to post $\text{TxOpen}$ on the blockchain before time $t$, User can claim both the refund $d^C_B$ and the compensation $d^S_B$ by posting $\text{TxRefund}$ and $\text{TxCompensation}$ on the blockchain, respectively. Obviously, in any case, if CSP cannot return a valid search result, User is able to claim enough compensation besides the search fee refund or penalty from CSP no matter how CSP behaves. Similarly, payment fairness can also be realized if User is malicious. Therefore, fair payment is enabled in TKSE without needing any TTP if $H$ is collision-resistant and ECDSA is unforgeable under chosen message attacks.

Theorem 4 (Compatibility): TKSE is compatible with the Bitcoin blockchain and the Ethereum blockchain.

Proof: It easily follows from the design details of TKSE in Section V that the operations, which have to be performed on blockchains such as hashing and ECDSA verification, are allowed by Bitcoin and Ethereum [44], [45]. Accordingly, compatibility is realized in TKSE.

B. PERFORMANCE ANALYSIS

In this section, we first make a feature comparison between TKSE and previous SSE schemes. Then, we evaluate the performance of TKSE in terms of the number of transactions.

1) FEATURE COMPARISON

In this section, we compare TKSE with [5], [21], [35], [37], [38] in terms of Privacy, User-side Verifiability, Server-side Verifiability, Payment Fairness, No TTP and Compatibility. We use the symbol "-" to represent that the corresponding property is not considered. As shown in Table 2, the scheme [21] cannot realize user-side verifiability, and server-side verifiability is only obtained in TKSE. In other words, TKSE is the first SSE scheme supporting two-side verifiability. Only schemes [35], [37], [38] and TKSE introduce blockchain technologies into SSE. However, only the scheme [35] and TKSE do not need any TTP, and only TKSE enables fair payment. Additionally, only TKSE is compatible with Bitcoin and Ethereum.

2) NUMBER OF TRANSACTIONS

The number of transactions in blockchain-based solutions has an important effect on performance. We further analyze and

<table>
<thead>
<tr>
<th>Schemes</th>
<th>Privacy</th>
<th>User-side Verifiability</th>
<th>Server-side Verifiability</th>
<th>Payment Fairness</th>
<th>No TTP</th>
<th>Compatiblity</th>
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<td>-</td>
<td>✗</td>
<td>-</td>
</tr>
<tr>
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<td>-</td>
<td>✗</td>
<td>-</td>
</tr>
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</tr>
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<td>✓</td>
<td>✓</td>
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<td>-</td>
</tr>
</tbody>
</table>

Note: Trusted banks are needed for fair payment.

The main is supposed to be honest to collect votes in the network, and some network nodes are supposed to be trustworthy initially.

The cloud server verifies a signature which is not related to the outsourced encrypted data.

Some network nodes are required to send file indexes and tokens to others.

The data owner may lose data without any compensation.

The string concatenation is involved in the transaction output script.
compare the number of transactions in the blockchain-based SSE scheme [35] (Li et al.’s scheme) and TKSE, in which TTP is not needed. We consider a data storage and search phase based on the Bitcoin blockchain in the normal case. Suppose the size of each document is 40 bytes, which is equal to the output size of the opcode OP_RETURN in Bitcoin. In [35], suppose SHA-1 is used. In the data storage phase, \( n_d + \frac{n_k}{d} \) transactions are created by User, where \( n_d \) is the number of documents and \( n_k \) is the number of keywords. In the data search phase, User and CSP create two and three transactions, respectively. As for TKSE, only one transaction \( \text{TxSearchSig} \) in involved in the Data Storage Phase. In the Data Search Phase, the transaction \( \text{TxSearchCommit} \) is created in the search commitment procedure. In the verification and payment procedure, transactions \( \text{TxVeriPay}, \text{TxSearchFee}, \text{TxGuaranty} \) and \( \text{TxOpen} \) are created. Note that \( \text{TxOpen} \) is created by CSP and it is not related to data search in the normal case. In the User Claim Phase, either the transaction \( \text{TxFine} \) or transactions \( \text{TxRefund} \) and \( \text{TxCompensation} \) are needed. Note that \( \text{TxRefund} \) and \( \text{TxCompensation} \) can be replaced with one transaction because they only need signatures of User. Similarly, \( \text{TxSearchFee} \) and \( \text{TxGuaranty} \) can be combined into one transaction. As shown in Figure 9, the number of involved transactions in TKSE is small and constant, which is not affected by the number of documents and keywords.

**VII. CONCLUSION**

Aiming to realize secure keyword search over encrypted data against malicious users and malicious cloud service providers, we proposed TKSE, a trustworthy keyword search scheme over encrypted cloud storage without needing any TTP. In TKSE, besides privacy and user-side verifiability, server-side verifiability is enabled for the first time in the literature, which protects honest cloud servers from being framed by malicious data owners in the data storage phase. In addition, fair payment is fulfilled based on blockchain technologies and hash functions without introducing any TTP. Our security analysis and performance evaluation indicated that TKSE is secure and efficient.

**REFERENCES**


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