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Low Detection Limit Time-Correlated Single Photon Counting Lifetime Analytical System for Point-of-Care Applications

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ABSTRACT Photon-counting analysis plays a key role in many areas, such as biology, chemistry, and medicine. In this paper, we present an integrated time-correlated single photon counting (TCSPC) lifetime analytical system with a complete signal path—from fluorophore excitation, emission detection, to lifetime extraction. The time-to-digital module of the proposed TCSPC system achieves a root-mean-square differential non-linearity of 4% of the least significant bit and a full width at half maximum temporal resolution from 121 to 145 ps within the 500-ns full-scale range. To evaluate the lifetime extraction and detection limit of the proposed TCSPC system, a wide variety of samples, such as fluorescein in water, coumarin 6 in dimethyl sulfoxide, and rhodamine 6G in water, each prepared in 14 concentrations from 0.5 nM (nanomolar, $10^{-9}$ mol/L) to 25 µM (micromolar, $10^{-6}$ mol/L), are tested. With the optimized hardware and firmware design, the proposed TCSPC system can accurately extract the fluorescence lifetime of fluorescein, coumarin 6, and rhodamine 6G down to the concentration of 1, 1, and 2.5 nM, respectively, significantly outperforming similar fluorescence lifetime analysis systems.

INDEX TERMS Non-invasive optical analysis, time-correlated single photon counting, low detection limit, fluorescence lifetime extraction.

I. INTRODUCTION

Fluorescence analysis has become an increasingly well-adopted technique in analytical chemistry, medical diagnostics, and biological research, recently many research works have been proposed to related areas [1]–[10]. As fluorescence analytical instruments are usually implemented in the compact system scale, it becomes increasingly difficult to provide good excitation rejection. The large background noise degrades signal to noise performance. Recently, lifetime techniques have gained wide interest as a way to address the above limitation, predicated on the fact that detection is typically performed when the pulsed excitation is in the off state. In addition, the lifetime of a fluorescence molecule is sensitive and specific to the surrounding chemical environment, rendering lifetime techniques selective analytical methods [11].

Fluorescent samples such as Fluorescein [12]–[16], Coumarin 6 [17]–[20] and Rhodamine 6G [21]–[25] have been used widely as biomarkers. For many in vivo experiments, increasing the concentration of fluorescent probes can precipitate molecules, cause cellular distortions, self-quenching, or induce cell death. Therefore, a low detection limit, which is defined as the lowest analyte concentration that the instrument can reliably obtain the fluorescence lifetime [26], is required in many fluorescence analysis experiments. Designing a compact, portable, and integrated system for sensing chemical and biological samples with a detection limit lower than those of conventional fluorescence lifetime analysis systems is the target of this work.

Fluorescence lifetime analysis techniques can be classified into frequency-domain and time-domain techniques. Frequency-domain techniques record the phase and amplitude of the signal as a function of frequency whereas time-domain techniques record the intensity of the signal as a function of time [27]. These two techniques require different hardware architectures resulting in different performance, suitable for various applications.

Using frequency domain techniques, fluorescence lifetimes can be determined by a phase-modulation technique.
A modulated light source is used to excite the fluorescent sample. The resulting emission signal from the sample has a similar but modulated and phase-shifted waveform in comparison to the excitation signal. Both characteristic modulation and phase-shift are determined by the lifetime of the fluorescence emission, therefore lifetime can be calculated from the observed modulation and phase-shift [28]. The frequency-domain fluorescence lifetime analysis techniques are compatible with tunable continuous-wave excitation source that seamlessly covers a wide spectral range. However, under weak photon emission from the sample, the accuracy of fluorescence lifetime detection is severely degraded.

Time domain techniques can generally be subdivided into time-gated photon counting and time-correlated single photon counting (TCSPC) [29]. Time-gated photon counting is used in combination with laser scanning to record fluorescence lifetime information at high efficiency. Time-gated technique operates on a timescale orders of magnitude greater than frequency domain methods [30]. The time-gated detector can reject most of the early arrival emitted photons [31], thus greatly reducing the amount of unfiltered excitation photons detected by the detector. However, the amplitudes and lifetime parameters of multiexponential decay profiles are difficult to obtain [32]. Moreover, the temporal resolution of existing time-gated photon counting implementations is generally limited. For instance, the histogram temporal resolution of time-resolved fluorescence analysis microsystem [33] and portable time-domain LED fluorimeter [34] are 450 ps and 250 ps, respectively, which are insufficient and can influence the accuracy of the lifetime measurements. This can be improved by using TCSPC.

With the advance of integrated electronics, TCSPC has been recently applied to fluorescence correlation spectroscopy [35], fluorescence lifetime imaging (FLIM), fluorescence resonance energy transfer (FRET) [11], [32], [36], [37], and other applications due to its high temporal resolution, high sensitivity, high counting efficiency, high signal-to-noise ratio (SNR) [38] and short measurement time. TCSPC measures the elapsed time between an excitation pulse (START) and the corresponding emission fluorescence photon arrival (STOP) repetitively with sub-nanosecond temporal resolution. After the detection of several photons, a histogram whose x-axis represents the elapsed time delay and y-axis represents the number of photons collected for each time delay is built. The shape of the histogram represents the optical signal emitted by the excited sample [39] and the lifetime of the fluorescence emission can be extracted from the histogram. The histogramming process avoids any time gating or wavelength scanning, thus yielding a better counting efficiency than the time-gated photon counting technique [37].

In terms of system building blocks, much work has been done to develop high-performance time-to-digital converters (TDCs) [40]–[44] or time-gated detectors [31], [45]–[48] and single-photon avalanche diodes (SPADs) [49], [50] recently. Also, photon counting systems for non-invasive fluorescence lifetime analysis have been proposed albeit with relatively low level of integration [5], [28], [34], [39], [51]–[56], but most of these designs neither present a convenient way to extract fluorescence lifetime nor verify the accuracy of the fluorescence lifetime measurement. There are also chip-level implementations of fluorescence lifetime measurement systems [33], [57], [58] with a high-level of integration and generally low power consumption. However, fluorescence lifetime measurements tend to be of low to medium volume applications, where discrete implementation has the advantage of a short production cycle, low startup cost, and large flexibility in implementing design revisions. Therefore, further improvements to discrete implementations of lifetime analytical systems combining data-acquisition with lifetime extraction is of great demand.

In this paper, we present a compact, low detection limit TCSPC system with fluorescence lifetime extraction. By using a digital TDC to sample and digitalize the elapsed time between excitation and emission, the system achieves a temporal resolution from 121 ps to 145 ps within the FSR of 300 ns for time-to-digital measurements. The conversion speed of the proposed TCSPC system is up to 160k samples per second (sp/s). Fluorescence lifetime extraction is achieved by employing the non-linear least square (NLLS) method [59]–[61] and experimentally demonstrated using different fluorescent samples. The detection limit is evaluated by Fluorescein in water, Coumarin 6 in Dimethyl sulfoxide (DMSO), and Rhodamine 6G in water, each prepared in 14 concentrations, from 0.5 nM (nanomolar, 10^{-9} mol/L) to 25 μM (micromolar, 10^{-6} mol/L), in order to introduce minimum influence of in vivo experiments. The proposed TCSPC system can accurately extract lifetime of Fluorescein in water, Coumarin 6 in DMSO and Rhodamine 6G in water down to the concentration of 1 nM, 1 nM, and 2.5 nM, respectively, significantly outperforming similar fluorescence lifetime analysis systems in terms of detection limit.

This paper is organized as follows. Section II discusses the theory of fluorescence lifetime extraction. Section III, IV, and V present the system architecture and implementation and experimental results, respectively. Section VI concludes the paper.

II. THEORY

Upon the removal of optical excitation from a fluorescence molecule, the emission typically follows a decaying profile, which is often fitted by negative multi-exponential functions [62]. Fluorescence lifetimes are the time constants of the multi-exponential decay. Therefore, the theoretical fluorescence decay $F(t)$ as a function of time $t$ is conventionally described by the multi-exponential equation [11], [38], given by

$$F(t) = \sum_{j=1}^{m} \alpha_j \exp(-t/\tau_j)$$  (1)
where \( m \) is the number of fluorescence lifetime components, \( \alpha_j \) and \( \tau_j \) are the decay amplitude and fluorescence lifetime of the \( j \)'th component, respectively. Fluorescence lifetime \( \tau \) is defined as the time when fluorescence intensity attenuates to \( 1/e \) of the initial intensity for a single exponential decay \( (m = 1) \) [63]. An accurate fluorescence lifetime measurement normally requires the instrument response function (IRF), \( h(t) \), which is measured using a reference sample that directs a small fraction of the excitation light into the detection path in advance. Then the measured fluorescence decay \( R(t) \) is measured when the reference sample is replaced by the fluorescent sample. \( R(t) \) contains the instrumental effect and is given by the convolution of \( F(t) \) with \( h(t) \) [11], [38], given by

\[
R(t) = F(t) \otimes h(t)
\] (2)

Therefore, the theoretical fluorescence decay \( F(t) \) is then obtained by the deconvolution of the measured fluorescence decay and the IRF [27], [64].

NLLS has been one of the most commonly used methods recently for the analysis of TCSPC data to estimate decay amplitude and fluorescence lifetime [65]. Therefore, it is employed in the proposed TCSPC system to extract lifetime of measured fluorescent samples. NLLS is achieved by evaluating the goodness-of-fit from the reduced chi-square error, given by

\[
\chi^2_r(t) = \frac{1}{a-b} \sum_{i=1}^{n} \frac{[R(t_i) - R_c(t_i)]^2}{\sigma_i^2}
\] (3)

where \( a \) is the number of data points, \( b \) is the number of estimated parameters, and \( \sigma_i \) is the standard deviation of the photon count in the \( i \)'th time bin [11], [38], [66]. A good fit is characterized by a value of \( \chi^2_r(t) \) close to 1. The residual between the measured and calculated decay curve should be randomly distributed around 0. For example, Preus [67] uses a simplex search method of Lagarias et al. [68] that successively minimizes the error \( \chi^2_r(t) \).

### III. SYSTEM ARCHITECTURE

The architectural block diagram of the proposed TCSPC system is shown in Fig. 1. A pulsed excitation light emitting diode (LED) excites the fluorescent analytes in a cylindrical cuvette. Due to Stokes' shift, the emitted photons have longer wavelengths than that of the excitation. With a thin-film filter filtering out the excitation photons, the emitted photons can be detected by the photon detector. The pulse signals of both the excitation source and the detector constitute a signal pair of the proposed TCSPC system. The system can be divided into four blocks, including micro-optics, time-to-digital module with signal conditioning circuit, microcontroller unit (MCU) and graphical user interface (GUI).

### IV. IMPLEMENTATION

Fig. 2 depicts top view and side view of the proposed TCSPC system. The system consists of a 35 mm diameter NanoLED excitation source and four stacked printed circuit boards (from top to bottom: detector, time-to-digital module, MCU and conditioning circuit). The sample is held in a cylindrical cuvette to be excited and analyzed. The pulse signals of excitation and emission are transmitted by coaxial cables via SMA connectors and a USB cable provides communication to a PC.

#### A. EXCITATION FILTERING AND OPTICAL CONSIDERATIONS

In a practical TCSPC system using a thin-film filter, excitation rejection is inadequate, thus, both emission and a portion of the excitation reach the detector. Therefore, the total number of photons reaching the detector active area \( N_{tot} \) is given by

\[
N_{tot} = N_{ex} + N_{em}
\] (4)

where \( N_{ex} \) and \( N_{em} \) are the numbers of unfiltered excitation and emitted photons reaching the detector, respectively. The relative emission intensity \( \eta_{em} \) can be defined as

\[
\eta_{em} = N_{em}/N_{tot}
\] (5)
According to the Beer-Lambert Law [69], \( N_{em} \) decreases with a reduction in the concentration of fluorescent sample. Therefore, as \( n_{em} \) reduces, the background caused by unfiltered excitation photons becomes significant, making the fluorescence lifetime difficult to extract.

Another phenomenon that influences lifetime extraction is photobleaching, a photochemical alteration caused by prolonged excitation of fluorescent molecules, a.k.a. fluorophores or dyes, leading to an eventual loss of their capacity to fluoresce [70]. Prolonged measurement not only reduces the emission intensity but also heats the electronic components of the system. Both the reduced emission intensity due to photobleaching and drift due to electronic components heating degrade the sensitivity of the system. Therefore, the proposed TCSPC system needs to be designed to increase conversion rate and to decrease the influence of temperature, key factors for achieving a low detection limit.

### B. EXCITATION SOURCE

TCSPC applications require a pulsed excitation source at the wavelength from the UV to blue as many organic dyes and quantum dots absorb light most efficiently at this wavelength range. UV is even better than blue for many probes, but UV has been shown to damage or harm biological samples [71]. Therefore, a pulsed excitation in the violet-blue spectral range is selected for the proposed TCSPC system.

The HORIBA NanoLED N-455 light source, a nanosecond LED with a pulse full width at half maximum (FWHM) of 1.3 ns, 455 ± 10 nm peak wavelength, 7 pJ per pulse energy, a maximum repetition rate of 1 MHz is driven by a dedicated driver integrated circuit. The output pulse signal is selectable between NIM-compatible (Vpp = −0.8 V) and TTL-compatible (Vpp = +2 V). All these features make NanoLED a suitable choice for compact fluorescence lifetime measurements.

### C. DETECTOR

Photomultiplier tubes (PMTs) and SPADs are the most widely used photon counting detection technologies to-date [72]. The proposed TCSPC system is designed to be compatible with both detectors, rendering the system suitable for a variety of applications. Therefore, a PMT and an SPAD are selected as the alternative detector of the proposed TCSPC system.

1) **PMT**

The HORIBA PPD 650 picosecond photon detection module featuring < 0.25 ns risetime PMT is chosen. The 8mm diameter PMT covers the spectral range between 230 and 700 nm, and the maximum detection efficiency reaches around 35% between 300 and 500 nm. With a less than 80 counts per second (cps) dark count rate, 125 ps temporal resolution, and selectable output pulse signal between NIM and TTL, the HORIBA PPD 650 is suitable for accurate fluorescence lifetime measurements.

2) **SPAD**

The IDQ ID101-50 CMOS silicon chip combining a 50 µm diameter single SPAD and an active quenching circuit with less than 50 ns deadtime is selected as an alternative detector. The SPAD covers the spectral range between 350 and 900 nm, and the maximum detection efficiency is measured to be 35% at 500 nm. With 100 cps dark count rate, 40 ps temporal resolution, 0.5% afterpulsing probability, and an output pulse signal of +5V Vpp, The IDQ ID101-50 is suitable for compact fluorescence lifetime applications.
3) TRADE-OFF

PMTs offer large active area (up to cm$^2$), no dead time, the ability to record low dark current (down to $10^{-8}$ A/cm$^2$) at no added cost, and negligible thermal noise of the load resistance respect to the quantum noise that the detected current already carries. But PMTs are relatively bulky and fragile components, difficult to be qualified for use in demanding environment such as space, nuclear, and high electromagnetic interference (EMI) [73]. On the other hand, SPADs have easy compatibility to the standard CMOS process, reduced junction transit time and jitter of the pulse response, and the capability to be unaffected by strong electromagnetic fields [74]. However, SPADs have a dead time following each detected event [73], typically stronger afterpulsing probability than in PMTs increasing the noise background, and smaller active area compared to PMTs decreasing the collection efficiency when the optical signal arises from a large area and wide emitting angle [75]. Therefore, PMTs or SPADs can be chosen according to the requirements of different TCSPC lifetime applications. In measurements that require portability, an SPAD can be chosen as the detector. When the optical signal is relatively weak, to obtain a sufficiently high SNR for good lifetime extraction accuracy, a PMT can be selected at the expense of bulkiness.

As depicted in Fig. 2, when an SPAD is selected as the detector, the size of the proposed TCSPC system is 73.5 mm (L) × 61.3 mm (W) × 92.6 mm (H). When a PMT is selected, the detector board with SPAD is replaced by a PMT mounted on the chassis, thus increasing the system size slightly to 107.5 mm (L) × 76.8 mm (W) × 136.2 mm (H).

D. TIME-TO-DIGITAL MODULE WITH SIGNAL CONDITIONING CIRCUIT

Time-to-digital module of TCSPC applications requires conversion with reliable pico-second temporal resolution. The Texas Instruments time-to-digital converter TDC7200 is selected to convert elapsed time between the input signal pair to digital values because of its temporal resolution, self-calibration and insensitivity to temperature. TDC7200 is a stopwatch integrated circuit with 55 ps least significant bit (LSB) resolution used to measure the elapsed time between a single event (an edge on START pin) and multiple subsequent events (an edge on STOP pin). An internal self-calibrated timer base inside TDC7200 compensates for drift over time and temperature. All these features make the TDC7200 specifically suitable for TCSPC lifetime measurement. The completion interrupt status of time-to-digital conversion is continuously checked by the MCU during the measurement. When a time-to-digital conversion has completed, the result is read into the MCU and the next conversion is initiated.

Since the output high voltages of the excitation source and the alternative detectors are not compatible with the TDC7200, a signal conditioning circuit with Texas Instruments LSF0102 two-channel bidirectional multi-voltage translator is designed as the interface between the input signal pair and the TDC module to satisfy signal compatibility. As depicted in Fig. 1, connectors C1, C2 between the signal conditioning circuit and time-to-digital module can be switched between “F” and “R” position to conduct TCSPC measurement in forward or reverse START-STOP mode.

E. MCU

The Texas Instruments low-power MCU MSP430F5529 is selected as the core controller of the system. The MCU also processes the TCSPC signals and relay data/user commands to/from the PC. After system initialization, the MCU continuously polls for START commands sent from the user, then controls the TDC7200 to obtain the elapsed time between the input signal pair. The conversion results within the user customized measurement range are considered valid, thus stored in the MCU before transmitting to the PC for further analysis. Upon receiving the STOP command, the MCU terminates the time-to-digital conversion, then lifetime extraction is performed. Approximately 2.7 seconds are required to extract the lifetime of $3.0 \times 10^7$ valid conversion results on a 2.27 GHz dual core CPU. By only keeping the valid conversion results, the system can achieve valid conversions up to 160k sps, which enables the system to achieve a low detection limit.

F. GRAPHICAL USER INTERFACE

For user convenience, the top-level system control is performed by a customized GUI, as shown in Fig. 3. The MATLAB script opens the communication through a virtual serial port via USB and sends out the control commands to trigger the configured measurement. During the measurement, conversion results are received through multiple packages via USB. Once the measurement is terminated by the user, all digitalized elapsed time data are...
saved into a file, with which fluorescence lifetime is subsequently extracted using NLLS method. Lifetime extraction has been implemented as post-processing computation to add flexibility in performance optimization of the system. In fact, the employed NLLS is a commonly used method for fluorescence lifetime extraction and has been shown to be readily implemented on the MCU and other embedded hardware [76], [77]. The measured IRF curve, fluorescence decay curve, NLLS fitting curve and the extracted fluorescence lifetime are displayed on the GUI. With a customized, user-friendly GUI, the TCSPC system can be conveniently controlled and operated.

V. EXPERIMENTAL RESULTS
Several tests are made to evaluate the performance of the proposed TCSPC system in terms of differential non-linearity (DNL), FWHM temporal resolution of the TDC module, and lifetime extraction, detection limit of the system.

A. DNL
1) SETUP
The DNL of TDC module of the proposed TCSPC system is assessed through the code density test. The employed setup consists of two pulse generators: one providing the STOP signal with a fixed rate and the other generates a random signal used as the START signal, where the START and STOP signals are uncorrelated [39], [53]. The code density test shows a distribution that reflects both the DNL of the system and the statistical noise of the input signal. Therefore, to have a reasonably flat START-STOP input signal distribution, at least 10K conversion results per histogram bin are needed to achieve a <1% statistical noise [5], [78].

2) RESULT
As depicted in Fig. 4, the measured distribution of the code density test is shown in Fig. 4, ranging between +9.7% and −8.5% of the LSB, with an average root mean square (RMS) value of 4% of LSB within the 500 ns FSR. The average results per histogram bin are $3 \times 10^4$, thus the statistical noise of signal distribution is 0.6%, which is negligible in relation to the overall distribution.

B. FWHM TEMPORAL RESOLUTION
1) SETUP
The temporal resolution of TDC module of the proposed TCSPC system is characterized by the FWHM of the response to a given time interval event [79]. To measure the FWHM temporal resolution, START-STOP signal pair is obtained by splitting the output of a pulse generator. A fixed START-STOP delay can be obtained by using a passive adjustable delay line along the STOP signal path in order not to introduce additional jitter.

FIGURE 5. Measured FWHM temporal resolution of TDC module of the proposed TCSPC system.

2) RESULT
As depicted in Fig. 5, the measured FWHM temporal resolution of TDC module of the proposed TCSPC system is about 121 ps in the first 121 ns of the FSR and then it starts to worsen, reaching 145 ps at the end of the 500 ns FSR. The worsening in FWHM temporal resolution at longer START-STOP delays is mainly caused by the superposition of non-linearity of delay elements inside the TDC7200 for longer START-STOP delays.

C. LIFETIME EXTRACTION
1) SETUP
The lifetime extraction performance of the proposed TCSPC system is experimentally validated by testing with 3 commercially available fluorescent samples, including Fluorescein (Sigma-Aldrich) in water, Rhodamine 6G (Shanghai Gold Wheat) in water and Coumarin 6 (Sigma-Aldrich) in DMSO. During the measurement, de-ionized water is used as a reference to acquire the IRF of the proposed TCSPC system, then de-ionized water is replaced with the testing fluorescent sample to measure the decay curve.
2) RESULT

Fig. 6 shows the measured IRF of TCSPC system and the decay curve of Fluorescein in water (5 µM). The FWHM of IRF is 1.35 ns and extracted fluorescence lifetime of Fluorescein in water with PMT and SPAD are 3.99 ns and 4.09 ns, respectively, compared to the specification value of 4.00 ns. Based on the same measurement protocol, two other commercial fluorescent samples are also measured as plotted in Fig. 7 and Fig. 8. The extracted fluorescence lifetime of Rhodamine 6G in water (5 µM) with PMT and SPAD are 4.04 ns and 4.07 ns, respectively, compared to the specification value of 4.00 ns. The extracted fluorescence lifetime of Coumarin 6 in DMSO (5 µM) with PMT and SPAD are 2.32 ns and 2.45 ns, respectively, compared to the specification value of 2.32 ns [80]. These results show that the proposed TCSPC system can extract lifetime of different fluorescent samples accurately.

D. DETECTION LIMIT

1) SETUP

In order to evaluate the detection limit of the proposed TCSPC system with PMT (SPAD) and compare it with similar fluorescence lifetime analysis systems [26], [28], [33], [34], [55], each of Fluorescein in water, Coumarin 6 in DMSO and Rhodamine 6G in water is prepared in 14 concentrations (from 0.5 nM to 25 µM) and measured for 8 times with fluorescence lifetime separately extracted. Then, average value $\bar{\tau}$ and standard deviation $\sigma$ of the extracted fluorescence lifetimes for each sample in 14 concentrations are calculated.
The statistical properties of the extracted lifetimes (ELTs) of the proposed TCSPC system with (a) SPAD and (b) PMT, and the theoretical lifetimes (TLTs) are also illustrated. Each of Fluorescein (Fluo) in water, Rhodamine 6G (Rh6G) in water, and Coumarin 6 (Cou6) in DMSO is prepared in 14 concentrations (0.5 nM, 1 nM, 2.5 nM, 5 nM, 10 nM, 25 nM, 50 nM, 100 nM, 250 nM, 500 nM, 750 nM, 1 µM, 5 µM, and 25 µM, respectively) and measured 8 times with fluorescence lifetime separately extracted. Then these data are used to calculate statistics, such as average fluorescence lifetime $\bar{\tau}$ and the standard deviation $\sigma$, and as a reference compared against time-gated fluorimeter of [34]. The detection limits of the proposed TCSPC system with PMT (SPAD) for Fluorescein in water, Coumarin 6 in DMSO and Rhodamine 6G in water are 1 nM (10 nM), 1 nM (5 nM) and 2.5 nM (5 nM), respectively. For samples having a concentration lower than the detection limit, the extracted fluorescence lifetime deviates from the factory-characterized value by greater than 5%. Whereas, for concentrations within the range of the system, it consistently provides extracted lifetime values that matches well with the reported value.

2) RESULT
The statistical properties of the extracted lifetimes of the proposed TCSPC system are shown in Fig. 9. The data suggest that the detection limits of the proposed TCSPC system with PMT (SPAD) for Fluorescein in water, Coumarin 6 in DMSO and Rhodamine 6G in water are 1 nM (10 nM), 1 nM (5 nM) and 2.5 nM (5 nM), respectively. When the samples are diluted less than the detection limits, the extracted fluorescence lifetime, e.g. the average value, begins to deviate from the specification value, with increased measurement variability.

The detection limit, error at detection limit, standard deviation at detection limit, number of channels, power consumption, and size of fluorescence lifetime analysis systems are compared in Table 1. The statistical properties of time-domain fluorimeter presented by Wang et al. [34] are also illustrated both in Fig. 9 and Table I with 0.5 µM detection limit for Fluorescein in water. The detection limit for CdSe/ZnS quantum dot samples of vertically integrated CMOS microsystem for time-resolved fluorescence analysis presented by Rae et al. [33], [55] is 0.01 µM. Portable phase fluorometer designed by Kissinger and Wilson [28] can extract fluorescence lifetime of Fluorescein in water down to the concentration of 7.5 µM. The lowest concentration experimentally injected for reliable lifetime measurement of Fluorescein in water is 1 nM for phase-sensitive fluorescence lifetime detection presented by He and Geng [26]. However, the deviation of the extracted fluorescent lifetime is greater than 5% and the standard deviation is larger than that of the proposed TCSPC system with PMT when the sample concentration is 1 nM. Therefore, the proposed TCSPC system significantly outperforms similar fluorescence lifetime analysis systems based on either time-gated photon counting or phase-modulated technique in terms of detection limit.

E. DISCUSSION
Experimental characterizations of lifetime extraction and detection limit show that the system performs better when a PMT is selected as the detector. The reason is that the PMT has a larger active area than the SPAD, thus obtaining...
TABLE 1. Comparison table of fluorescence lifetime analysis systems in terms of detection limit.

<table>
<thead>
<tr>
<th>System</th>
<th>This work&lt;sup&gt;a&lt;/sup&gt;</th>
<th>This work&lt;sup&gt;b&lt;/sup&gt;</th>
<th>H. Wang et al. [34]</th>
<th>B. R. Rae et al. [33, 35]</th>
<th>J. Kissinger et al. [28]</th>
<th>Y. He et al. [26]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Detection Limit</td>
<td>1 nM</td>
<td>5 nM</td>
<td>0.5 µM</td>
<td>0.01 µM</td>
<td>7.5 µM</td>
<td>1 nM</td>
</tr>
<tr>
<td>Error at detection limit/Theoretical value (%)</td>
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<td>6.2</td>
<td>0</td>
<td>N/A</td>
<td>N/A</td>
<td>6.25</td>
</tr>
<tr>
<td>Standard deviation at detection limit/Theoretical value (%)</td>
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<td>0.9</td>
<td>5</td>
<td>N/A</td>
<td>N/A</td>
<td>5.75</td>
</tr>
<tr>
<td>Number of channels</td>
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<td>1</td>
<td>1</td>
<td>64</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>Power consumption</td>
<td>Medium</td>
<td>Medium</td>
<td>Medium</td>
<td>Small</td>
<td>Small</td>
<td>N/A</td>
</tr>
<tr>
<td>Size</td>
<td>Medium</td>
<td>Medium</td>
<td>Medium</td>
<td>Small</td>
<td>Small</td>
<td>N/A</td>
</tr>
</tbody>
</table>

<sup>a</sup>For Fluorescein in water when a PMT is selected as the detector.

<sup>b</sup>For Coumarin 6 in DMSO when an SPAD is selected as the detector.

a better SNR. This accuracy-size trade-off is elaborated in Section IV.C.3. Nonetheless, the performance achievable by the SPAD is also sufficient for a variety of practical applications.

VI. CONCLUSION

In this paper, a low detection limit TCSPC system with fluorescence lifetime extraction is presented. With optimized hardware and firmware design, the proposed TCSPC system can extract fluorescence lifetime of Fluorescein, Coumarin 6, and Rhodamine 6G down to the concentration of 1 nM, 1 nM and 2.5 nM, respectively, demonstrating a new level of sensitivity for singlet oxygen, "J. Am. Chem. Soc.," vol. 123, no. 11, pp. 2530–2536, Mar. 2001.

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